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# Eleat Transfer

A Practical Approach

YUNUS A. ÇENGEL

# HEAT TRANSFER

## A PRACTICAL APPROACH

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## McGraw-Hill Higher Education

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#### **HEAT TRANSFER: A PRACTICAL APPROACH**

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This book is printed on acid-free paper.

domestic

234567890DOC/DOC0987654321

international

1234567890DOC/DOC0987654321

#### ISBN 0-07-011505-2

Vice president and editorial director: Kevin T. Kane

Publisher: Tom Casson

Senior sponsoring editor: Debra Riegert Marketing manager: John Wannemacher

Project manager: Gladys True

Production supervisor: Heather D. Burbridge

Designer: Matthew Baldwin

Cover designer: Ellen Pettengell, Ellen Pettengell Design

Compositor: GAC/Indianapolis Typeface: 10.5/12 Times Roman

Printer: R. R. Donnelley & Sons Company

#### Library of Congress Cataloging-in-Publication Data

Cengel, Yunus A.

Heat transfer: a practical approach / Yunus A. Çengel

p. cm.

Includes index.

ISBN 0-07-01105-2

1. Heat—Transmission. 2. Heat—Transmission—Industrial

applications. I. Title.

QC320.C46 1997

621.402'2—dc21

97-6640

#### INTERNATIONAL EDITION

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When ordering the title, use ISBN -0-7-115223-7

If interested in ordering the book with the EES problems disk use ISBN 0-07-561176-7 since the book will be available in two different versions.

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# Heat Exchangers

Heat exchangers are devices that facilitate the exchange of heat between two fluids that are at different temperatures while keeping them from mixing with each other. Heat exchangers are commonly used in practice in a wide range of applications, from heating and air-conditioning systems in a household, to the common of the control of the common of th

Heat transfer in a heat exchanger usually involves convection in each fluid and conduction through the wall separating the two fluids. In the analysis of heat exchangers, it is convenient to work with an overall heat transfer coefficient U that accounts for the contribution of all these effects on heat transfer. The rate of heat transfer between the two fluids at a location in a heat exchanger depends on the magnitude of the temperature difference at that location, which varies along the heat exchanger. In the analysis of heat exchangers, it is usually convenient to work with the logarithmic mean temperature difference LMTD, which is an equivalent mean temperature difference between the two fluids for the entire heat exchanger.

Heat exchangers are manufactured in a variety of types, and thus we start this chapter with the classification of heat exchangers. We then discuss the determination of the overall heat transfer coefficient in heat exchangers, and the logarithmic mean temperature difference LMTD for some configurations. We then introduce the correction factor F to account for the deviation of the mean temperature difference from the LMTD in complex configurations. Next we discuss the effectiveness-NTU method, which enables us to analyze heat exchangers when the outlet temperatures of the fluids are not known. Finally, we discuss the selection of heat exchangers.

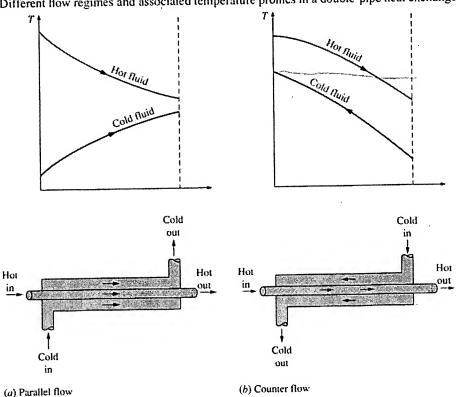
#### 10-1 TYPES OF HEAT EXCHANGERS

Different heat transfer applications require different types of hardware and different configurations of heat transfer equipment. The attempt to match the heat transfer hardware to the heat transfer requirements within the specific constraints has resulted in numerous types of innovative heat exchange designs.

The simplest type of heat exchanger consists of two concentric pipesof different diameters, as shown in Figure 10-1, called the double-pipeheat exchanger. One fluid in a double-pipe heat exchanger flows through the smaller pipe while the other fluid flows through the annular space between the two pipes. Two types of flow arrangement are possible in a double-pipe heat exchanger: in parallel flow, both the hot and cold fluids enter the heat exchanger at the same end and move in the same direction. In counter flow on the other hand, the hot and cold fluids enter the heat exchanger at opposite ends and flow in opposite directions.

Another type of heat exchanger, which is specifically designed to realize a large heat transfer surface area per unit volume, is the compact heat exchanger. The ratio of the heat transfer surface area of a heat exchanger to its

FIGURE 10-1
Different flow regimes and associated temperature profiles in a double-pipe heat exchanger.



Types of Heat Exchangers

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of two concepts.

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called the area density  $\beta$ . A heat exchanger with  $\beta > 700 \text{ m}^2/\text{m}^3$  is classified as being compact. Examples of compact heat car radiators ( $\beta \approx 1000 \text{ m}^2/\text{m}^3$ ), glass ceramic gas turbine the car radiators ( $\beta \approx 6000 \text{ m}^2/\text{m}^3$ ), the regenerator of a Stirling engine there is  $\beta \approx 6000 \text{ m}^2/\text{m}^3$ ), and the human lung ( $\beta \approx 20.000 \text{ m}^2/\text{m}^3$ ). Compact heat ransfer rates between two fluids in enable us to achieve high heat transfer rates between two fluids in the weight and volume of heat exchangers (Fig. 10-2).

the weight and votation of their exchangers (Fig. 10-2).

Ings surfaces area in compact heat exchangers is obtained by trues spaced thin plate or corrugated fins to the walls separating clads. Compact heat exchangers are commonly used in gas-to-gas hiquid (or liquid-to-gas) heat exchangers to counteract the low heat efficient associated with gas flow with increased surface area. In a which is a water-to-air compact heat exchanger, for example, it that him are attached to the air side of the tube surface.

apact heat exchangers, the two fluids usually move perpendicular ther, and such flow configuration is called cross-flow. The cross-ther classified as unmixed and mixed flow, depending on the flow iden, as shown in Figure 10-3. In (a) the cross-flow is said to be since the plate fins force the fluid to flow through a particular interfining prevent it from moving in the transverse direction (i.e., parallel fine cross-flow in (b) is said to be mixed since the fluid now is make in the transverse direction. Both fluids are unmixed in a car the presence of mixing in the fluid can have a significant effect on transfer characteristics of the heat exchanger.

To us the most common type of heat exchanger in industrial applica-

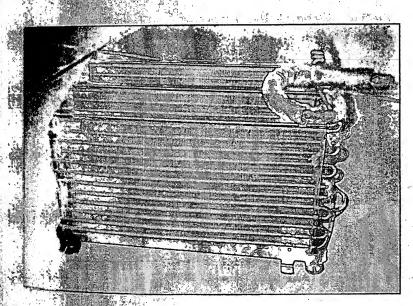


FIGURE 10-2

A gas-to-liquid compact heat exchanger for a residential air-conditioning system.

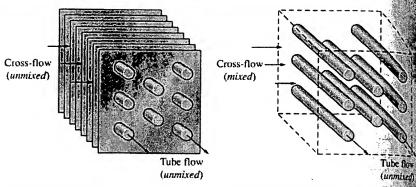


FIGURE 10-3

Different flow configurations in crossflow heat exchangers.

(a) Both fluids unmixed

(b) One fluid mixed, one fluid unmixed

tube heat exchangers contain a large number of tubes (sometimes several hundred) packed in a shell with their axes parallel to that of the shell. Heat transfer takes place as one fluid flows inside the tubes while the other fluid flows outside the tubes through the shell. Baffles are commonly placed in the shell to force the shell-side fluid to flow across the shell to enhance heat transfer and to maintain uniform spacing between the tubes. Despite their widespread use, shell-and-tube heat exchangers are not suitable for use in automotive, aircraft, and marine applications because of their relatively large size and weight. Note that the tubes in a shell-and-tube heat exchanger open to some large flow areas called headers at both ends of the shell, where the tube-side fluid accumulates before entering the tubes and after leaving them.

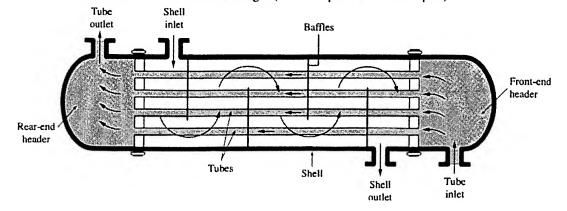
Shell-and-tube heat exchangers are further classified according to the number of shell and tube passes involved. Heat exchangers in which all the tubes make one U-turn in the shell, for example, are called *one-shell pass and two-tube pass* heat exchangers. Likewise, a heat exchanger that involves two passes in the shell and four passes in the tubes is called a *two-shell pass and four-tube pass* heat exchanger (Fig. 10-5).

An innovative type of heat exchanger that has found widespread use if the plate and frame (or just plate) heat exchanger, which consists of a series

#### FIGURE 10-4

1

The schematic of a shell-and-tube heat exchanger (one-shell pass and one-tube pass).



of plates with conducted by two hot fluids heal exchangers computing more plapplications, processe pressure.

Another type hot and cold flui heat exchanger.
porous mass the wire mesh. Hot a Heat is transferring the flow of the flow of the cold medium.

The dynami

FIGURE 10-6

A plate-and-fram



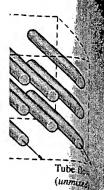
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FIGURE 10-6

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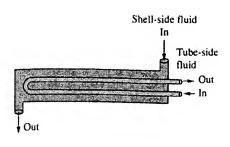
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of plates with corrogated flat flow passages (Fig. 10-6). The hot and cold fluids flow in alternate passages, and thus each cold fluid stream is surrounded by two hot fluid streams, resulting in very effective heat transfer. Also, plate heat exchangers can grow with increasing demand for heat transfer by simply mounting more plates. They are well suited for liquid-to-liquid heat exchange applications, provided that the hot and cold fluid streams are at about the same pressure.

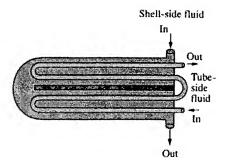
Another type of heat exchanger that involves the alternate passage of the hot and cold fluid streams through the same flow area is the regenerative heat exchanger. The static-type regenerative heat exchanger is basically a porous mass that has a large heat storage capacity, such as a ceramic wire mesh. Hot and cold fluids flow through this porous mass alternatively. Heat is transferred from the hot fluid to the matrix of the regenerator during the flow of the hot fluid, and from the matrix to the cold fluid during the flow of the cold fluid. Thus, the matrix serves as a temporary heat storage medium.

The dynamic-type regenerator involves a rotating drum and continuous flow of the hot and cold fluid through different portions of the drum so that

A plate-and-frame liquid-to-liquid heat exchanger (courtesy of Trante Corp.).



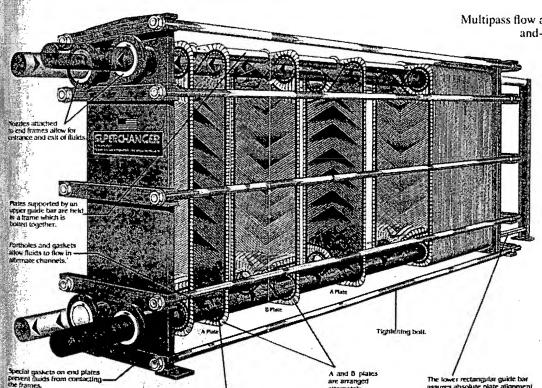
(a) One-shell pass and two-tube passes

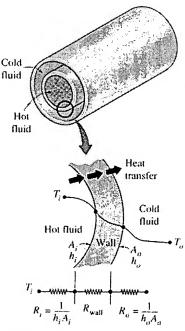


(b) Two-shell passes and four-tube passes

#### FIGURE 10-5

Multipass flow arrangements in shelland-tube heat exchangers.



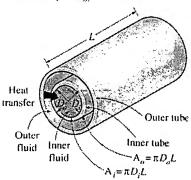


#### FIGURE 10-7

Thermal resistance network associated with heat transfer in a double-pipe heat exchanger.

#### FIGURE 10-8

The two heat transfer surface areas associated with a double-pipe heat exchanger (for thin tubes,  $D_i \approx D_o$  and thus  $A_i \approx A_o$ ).



any portion of the drum passes periodically through the hot stream, stored heat, and then through the cold stream, rejecting this stored heat. Again to drum serves as the medium to transport the heat from the hot to the cold has stream.

Heat exchangers are often given specific names to reflect the specific application for which they are used. For example, a *condenser* is a heat exchanger in which one of the fluids gives up heat and condenses as it float through the heat exchanger. A *boiler* is another heat exchanger in which one of the fluids absorbs heat and vaporizes. A *space radiator* is a heat exchanger that transfers heat from the hot fluid to the surrounding space by radiation.

#### 10-2 THE OVERALL HEAT TRANSFER COEFFICIENT

A heat exchanger typically involves two flowing fluids separated by a sold wall. Heat is first transferred from the hot fluid to the wall by *convection*, through the wall by *conduction*, and from the wall to the cold fluid again by convection. Any radiation effects are usually included in the convection has transfer coefficients.

The thermal resistance network associated with this heat transfer process involves two convection and one conduction resistances, as shown in Figure 10. Here the subscripts i and o represent the inner and outer surfaces of the inner tube. For a double-pipe heat exchanger, we have  $A_i = \pi D L$  and  $A_o = \pi D L$  and the thermal resistance of the tube wall in this case is

$$R_{\text{wall}} = \frac{\ln (D_o/D_i)}{-2\pi kL}$$

where k is the thermal conductivity of the wall material and L is the length the tube. Then the *total thermal resistance* becomes

$$R = R_{\text{total}} = R_i + R_{\text{wall}} + R_o = \frac{1}{h_i A_i} + \frac{\ln(D_o/D_i)}{2\pi kL} + \frac{1}{h_o A_o} \chi^{(0)}$$

The  $A_i$  is the area of the *inner surface* of the wall that separates the fluids, and  $A_o$  is the area of the outer surface of the wall. In other words and  $A_o$  are surface areas of the separating wall wetted by the inner and outer fluids, respectively. When one fluid flows inside a circular tube the other outside of it, we have  $A_i = \pi D_i L$  and  $A_o = \pi D_o L$  (Fig. 10-8).

In the analysis of heat exchangers, it is convenient to combine although thermal resistances in the path of heat flow from the hot fluid to the convenient one into a single resistance R, as we discussed in Chapter 3, and to expect the rate of heat transfer between the two fluids as

$$\dot{Q} = \frac{\Delta T}{R_s} = UA\Delta T = U_f A_f \Delta T = U_s A_s \Delta T \qquad (18)$$

where U is the overall heat transfer coefficient, whose unit is which is identical to the unit of the ordinary convection coefficient U celing  $\Delta T$ . Equation 10-3 reduces to

Pohaps you are wo  $V_a$  and  $U_o$  for a hea wo heat transfer sugh other.

Note that  $U_iA_i$ :
heat transfer coeffice on which it is based that the wall is finned side is severa. When the wall is in the tube materia he tube is negligible to almost identical masser coefficient.

where  $U \approx U_c \approx 1$ nside and outside chions discussed The overall hea maller convec When one Ther (say,  $h_i \ll h_o$ Wiler heat transfe id seriously impo ge of the fluids is mmonly used on Outer on that side Representative Mile 10-1. Note Wm2.°C for g exchangers tha very low ther thigh heat trans When the tube densfer surfac

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L is the length of

$$-\frac{1}{h_o A_o}$$
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$$\frac{1}{UA} = \frac{1}{U_i A_i} = \frac{I}{U_o A_o} = R = \frac{1}{h_i A_i} + R_{wall} + \frac{1}{h_o A_o}$$
(10-4)

Perhaps you are wondering why we have *two* overall heat transfer coefficients  $U_i$  and  $U_o$  for a heat exchanger. The reason is that every heat exchanger has two heat transfer surface areas  $A_i$  and  $A_o$ , which, in general, are not equal to each other.

Note that  $U_iA_i = U_oA_o$ , but  $U_i \neq U_o$  unless  $A_i = A_o$ . Therefore, the overall heat transfer coefficient U of a heat exchanger is meaningless unless the area on which it is based is specified. This is especially the case when one side of the tube wall is finned and the other side is not, since the surface area of the finned side is several times that of the unfinned side.

When the wall thickness of the tube is small and the thermal conductivity of the tube material is high, as is usually the case, the thermal resistance of the tube is negligible  $(R_{\text{wall}} \approx 0)$  and the inner and outer surfaces of the tube are almost identical  $(A_i \approx A_o \approx A)$ . Then Equation 10-4 for the overall heat transfer coefficient simplifies to

$$\frac{1}{U} \approx \frac{1}{h_i} + \frac{1}{h_o} \tag{10-5}$$

where  $U \approx U_i \approx U_o$ . The individual convection heat transfer coefficients inside and outside the tube,  $h_i$  and  $h_o$ , are determined using the convection relations discussed in earlier chapters.

The overall heat transfer coefficient U in Equation 10-5 is dominated by the smaller convection coefficient, since the inverse of a large number is small. When one of the convection coefficients is much smaller than the other (say,  $h_i \ll h_o$ ), we have  $1/h_i \gg 1/h_o$ , and thus  $U \approx h_i$ . Therefore, the smaller heat transfer coefficient creates a bottleneck on the path of heat flow and seriously impedes heat transfer. This situation arises frequently when one of the fluids is a gas and the other is a liquid. In such cases, fins are commonly used on the gas side to enhance the product UA and thus the heat transfer on that side.

Representative values of the overall heat transfer coefficient U are given in Table 10-1. Note that the overall heat transfer coefficient ranges from about  $10 \text{ W/m}^2$ . °C for gas-to-gas heat exchangers to about  $10,000 \text{ W/m}^2$ . °C for best exchangers that involve phase changes. This is not surprising, since gases have very low thermal conductivities, and phase-change processes involve very high heat transfer coefficients.

When the tube is finned on one side to enhance heat transfer, the total leat transfer surface area on the fined side becomes

$$A = A_{\text{total}} = A_{\text{fin}} + A_{\text{unfinned}} \tag{10-6}$$

where  $A_{\rm fin}$  is the surface area of the fins and  $A_{\rm unfinned}$  is the area of unfinned Portion of the tube surface. For short fins of high thermal conductivity, we can use this total area in the convection resistance relation  $R_{\rm conv}=1/hA$  since the fins in this case will be very nearly isothermal. Otherwise, we should determine the effective surface are A from

The Overall Heat Transfer Coefficient

**TABLE 10-1** 

Representative values of the overall heat transfer coefficients in heat exchangers

Type of heat exchanger	U, W/m2 · °C+
Water-to-water	850-1700
Water-to-oil	100–350
Water-to-gasoline or kerosene	300-1000
Feedwater heaters	1000-8500
Steam-to-light fuel oil	200–400
Steam-to-heavy fuel oil	50-200
Steam condenser	1000-6000
Freon condenser (water cooled)	300–1000
Ammonia condenser (water cooled)	800–1400
Alcohol condensers (water cooled)	250–700
Gas-to-gas	10–40
Water-to-air in finned tubes (water in tubes)	30-601
(1.2.2.)	400-850 <sup>1</sup>
Steam-to-air in finned tubes (steam in tubes)	30-300 <sup>†</sup>
- Control of the cont	
	400-4000

<sup>&</sup>quot;Multiply the listed values by 0.176 to convert them to Btu/h · ft² · °F.

$$A = A_{\text{unfinned}} + \eta_{\text{fin}} A_{\text{fin}} \tag{10-7}$$

where  $\eta_{fin}$  is the fin efficiency. This way, the temperature drop along the fins is accounted for. Note that  $\eta_{fin}=1$  for isothermal fins, and thus Equation 10-7 reduces to Equation 10-6 in that case.

#### **Fouling Factor**

The performance of heat exchangers usually deteriorates with time as a result of accumulation of deposits on heat transfer surfaces. The layer of deposits represents additional resistance to heat transfer and causes the rate of heat transfer in a heat exchanger to decrease. The net effect of these accumulations on heat transfer is represented by a fouling factor  $R_f$ , which is a measure of the thermal resistance introduced by fouling.

The most common type of fouling is the precipitation of solid deposits in a fluid on the heat transfer surfaces. You can observe this type of fouling even in your house. If you check the inner surfaces of your teapot after prolonged use, you will probably notice a layer of calcium-based deposits of the surfaces at which boiling occurs. This is especially the case in areas where the water is hard. The scales of such deposits come off by scratching, and the surfaces can be cleaned of such deposits by chemical treatment. Now imaginations are surfaces can be cleaned of such deposits by chemical treatment.

hose mineral depo exchanger (Fig. 10 passage area and the power and process amoved before it in particles in the flu create similar problem.

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In applications in the design and s be necessary to self-insure that it meets occurs. The period are additional pena

The fouling fa treases with time a The fouling factor the fluids, as well a superature and de The overall head faces and needs both the inner and tube heat exchange

<sup>†</sup>Based on air-side surface area.

<sup>&</sup>lt;sup>1</sup>Based on water- or steam-side surface area.

The Overall Heat Transfer Coefficient

W/m2.°C 850-1700 100-350 300-1000 1000-8500 200-400 50-200 000-6000 300-1000 800-1400 250-700 10-40 30-60<sup>†</sup> 400-8501 30-300 400-4000

(107)

drop along the fins and thus Equation

with time as a result ne layer of deposits ses the rate of heat of these accumulawhich is a measure

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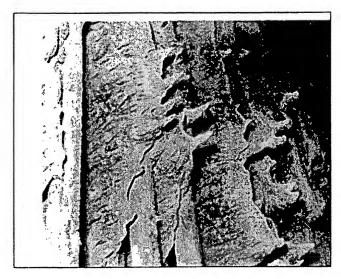


FIGURE 10-9

Precipitation fouling of ash particles on superheater tubes (from Steam, Its Generation, and Use, Babcock and Wilcox Co., 1978).

those mineral deposits forming on the inner surfaces of fine tubes in a heat exchanger (Fig. 10-9) and the detrimental effect it may have on the flow passage area and the heat transfer. To avoid this potential problem, water in power and process plants is extensively treated and its solid contents are emoved before it is allowed to circulate through the system. The solid ash particles in the flue gases accumulating on the surfaces of air preheaters create similar problems.

Another form of fouling, which is common in the chemical process industry, is corrosion and other chemical fouling. In this case, the surfaces are fouled by the accumulation of the products of chemical reactions on the surfaces. This form of fouling can be avoided by coating metal pipes with glass or using plastic pipes instead of metal ones. Heat exchangers may also be fouled by the growth of algae in warm fluids. This type of fouling is called hielogical fouling and can be prevented by chemical treatment.

In applications where it is likely to occur, fouling should be considered in the design and selection of heat exchangers. In such applications, it may be necessary to select a larger and thus more expensive heat exchanger to ensure that it meets the design heat transfer requirements even after fouling occurs. The periodic cleaning of heat exchangers and the resulting down time are additional penalties associated with fouling.

The fouling factor is obviously zero for a new heat exchanger and increases with time as the solid deposits build up on the heat exchanger surface. The fouling factor depends on the *operating temperature* and the *velocity* of the fluids, as well as the length of service. Fouling increases with *increasing temperature* and *decreasing velocity*.

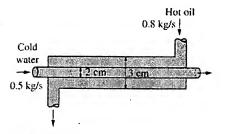
The overall heat transfer coefficient relation given above is valid for clean surfaces and needs to be modified to account for the effects of fouling on both the inner and the outer surfaces of the tube. For an unfinned shell-and-ube heat exchanger, it can be expressed as

**TABLE 10-2** 

Representative fouling factors (thermal resistance due to fouling for a unit surface area)

Fluid	R <sub>t</sub> , m²√°C/W
Distilled water, sea	
water, river water,	
boiler feedwater:	
Below 50°C	0.0001
Above 50°C	0.0002
Fuel oil	0.0009
Steam (oil-free)	0.0001
Refrigerants (liquid)	0.0002
Refrigerants (vapor)	0.0004
Alcohol vapors	0.0001
Air	0.0004

Source: Tubular Exchange Manufacturers Association.



**FIGURE 10-10** 

Schematic for Example 10-1.

$$\frac{1}{UA} = \frac{1}{U_i^2 A_i} = \frac{1}{U_o A_o} = R = \frac{1}{h_i A_i} + \frac{R_{f,i}}{A_i} + \frac{\ln(D_o^2/D_i)}{2\pi k L_c^2} + \frac{R_{f,o}}{A_o} + \frac{1}{h_i A_i}$$
(10-8)

where  $A_i = \pi D_i L$  and  $A_o = \pi D_o L$  are the areas of inner and outer surfaces and  $R_{fi}$  and  $R_{fo}$  are the fouling factors at those surfaces.

Representative values of fouling factors are given in Table 10-2. More comprehensive tables of fouling factors are available in handbooks. As you would expect, considerable uncertainty exists in these values, and they should be used as a guide in the selection and evaluation of heat exchangers to account for the effects of anticipated fouling on heat transfer. Note that most fouling factors in the table are of the order of  $10^{-4}$  m<sup>2</sup> · °C/W, which is equivalent to the thermal resistance of a 0.2-mm-thick limestone layer  $(k = 2.9 \text{ W/m} \cdot ^{\circ}\text{C})$  per unit surface area. Therefore, in the absence of specific data, we can assume the surfaces to be coated with 0.2 mm of limestone as a starting point to account for the effects of fouling.

#### **EXAMPLE 10-1** Overall Heat Transfer Coefficient of a Heat Exchanger

Hot oil is to be cooled in a double-tube counter-flow heat exchanger. The copper inner tube has a diameter of 2 cm and negligible thickness. The inner diameter of the outer tube (the shell) is 3 cm. Water flows through the tube at a rate of 0.5 kg/s, and the oil through the shell at a rate of 0.8 kg/s. Taking the average temperatures of the water and the oil to be 45°C and 80°C, respectively, delermine the overall heat transfer coefficient of this heat exchanger.

**Solution** Hot oil is cooled by water in a double-tube counterflow heat 82 changer. The overall heat transfer coefficient is to be determined.

Assumptions 1 The thermal resistance of the inner tube is negligible since the tube material is highly conductive and its thickness is negligible. 2 Both the oil and water flow are fully developed. 3 Proberties of the oil and water are constant.

Properties The properties of water at 45°C are (Table A-9)

$$\rho = 990 \text{ kg/m}^3$$
 Pr = 3.91  
 $k = 0.637 \text{ W/m} \cdot ^{\circ}\text{C}$   $\nu = \mu/\rho = 0.602 \times 10^{-6} \text{ m}^2/\text{s}$ 

The properties of oil at 80°C are (Table A-10).

$$p = 852 \text{ kg/m}^3$$
  $Pr = 490$   
 $k = 0.138 \text{ W/m} \cdot {}^{\circ}\text{C}$   $v = 37.5 \times 10^{-6} \text{ m}^2/\text{s}$ 

Analysis The schematic of the heat exchanger is given in Figure 10-10-10 overall heat transfer coefficient *U* can be determined from Equation 10-5

$$\frac{1}{U} \approx \frac{1}{h_I} + \frac{1}{h_o}$$

where  $h_i$  and  $h_o$  are the convection heat transfer coefficients inside and out the tube, respectively, which are to be determined using the forced convergence relations discussed in Chapter 6.

The hydraulic diameter for a circular tube is the diameter of the tube  $D_h = D = 0.02$  m. The average velocity of water in the tube and the number are

 $V_m = \frac{n}{pA}$ 

and

which is greater the line flow to be fully

$$Nu = \frac{hD_h}{k}$$

Then,

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$$=\frac{m_0}{pA_0} = \frac{1}{p[\frac{1}{4}]}$$

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ssion Note

$$\frac{1}{c} = \frac{m}{\rho(\frac{1}{4}\pi D^2)} = \frac{0.5 \text{ kg/s}}{(990 \text{ kg/m}^3)[\frac{1}{4}\pi (0.02 \text{ m})^2]} = 1.61 \text{ m/s}$$

The Overall Heat Transfer Coefficient

$$Re = \frac{V_m D_n}{v} = \frac{(1.61 \text{ m/s})(0.02 \text{ m})}{0.602 \times 10^{-6} \text{ m}^2/\text{s}} = 53,490$$

regien than 4000. Therefore, the flow of water is turbulent. Assuming the fully developed, the Nusselt number can be determined from

$$\frac{hD_0}{2} = 0.023 \, \text{Re}^{0.8} \text{Pr}^{0.4} = 0.023(53,490)^{0.8}(3.91)^{0.4} = 240.6$$

$$h = \frac{k}{D} \frac{\text{Nu}}{\sqrt{1 - \frac{1}{2}}} = \frac{0.637 \text{ W/m} \cdot ^{\circ}\text{C}}{0.02 \text{ m}} (240.6) = 7663 \text{ W/m}^{2} \cdot ^{\circ}\text{C}$$

we repeat the analysis above for oil. The properties of oil at 80°C are

$$p = 852 \text{ kg/m}^3$$
  $v = 37.5 \times 10^{-6} \text{ m}^2/\text{s}$   $k = 0.138 \text{ W/m} \cdot ^{\circ}\text{C}$   $Pr = 490$ 

ulc diameter for the annular space is

$$D_h^2 = D_o - D_i = 0.03 - 0.02 = 0.01$$
m

ge velocity and the Reynolds number in this case are

$$\frac{m}{p[\frac{1}{4}\pi(D_o^2 - D_i^2)]} = \frac{0.8 \text{ kg/s}}{(852 \text{ kg/m}^3)[\frac{1}{4}\pi(0.03^2 - 0.02^2)] \text{ m}^2} = 2.39 \text{ m/s}$$

Re 
$$=\frac{V_m D_h}{v} = \frac{(2.39 \text{ m/s})(0.01 \text{ m})}{37.5 \times 10^{-6} \text{ m}^2/\text{s}} = 637$$

has than 4000. Therefore, the flow of oil is laminar. Assuming fully develuable Nusselt number on the tube side of the annular space Nu, corregion  $D_1/D_0 = 0.02/0.03 = 0.667$  can be determined from Table 10-3 by

$$Nu = 5.45$$

$$b_0 = \frac{k}{D_0} \text{Nu} = \frac{0.138 \text{ W/m} \cdot ^{\circ}\text{C}}{0.01 \text{ m}} (5.45) = 75.2 \text{ W/m}^2 \cdot ^{\circ}\text{C}$$

in Highlighter

overall heat transfer coefficient for this heat exchanger becomes

$$\frac{1}{11} = \frac{1}{10} = 74.5 \text{ W/m}^2 \cdot ^{\circ}\text{C}$$

$$\frac{1}{10} = \frac{1}{100} = 74.5 \text{ W/m}^2 \cdot ^{\circ}\text{C}$$

Note that  $U \approx h_o$  in this case, since  $h_i \gg h_o$ . This confirms our earlier that the overall heat transfer coefficient in a heat exchanger is

**TABLE 10-3** 

Nusselt number for fully developed laminar flow in a circular annulus with one surface insulated and the other isothermal

$D_i/D_o$	Nui	Nu <sub>a</sub>
0.00	******	3.66
0.05	17.46	4.06
0.10	11.56	4.11
0.25	7.37	4.23
0.50	5.74	4.43
1.00	4.86	4.86

Source: Kays and Perkins, Ref. 8.

the two values is large. To improve the overall heat transfer coefficient and thus the heat transfer in

this heat exchanger, we must use some enhancement techniques on the oil side: such as a finned surface.

dominated by the smaller heat transfer coefficient when the difference between

#### **EXAMPLE 10-2** Effect of Fouling on the Overall Heat Transfer Coefficient

A double-pipe (shell-and-tube) heat exchanger is constructed of a stainless steel ( $k = 15.1 \text{ W/m} \cdot ^{\circ}\text{C}$ ) inner tube of inner diameter  $D_i = 1.5 \text{ cm}$  and outer diameter  $D_o = 1.9$  cm and an outer shell of inner diameter 3.2 cm. The convection heat transfer coefficient is given to be h<sub>i</sub> = 800 W/m<sup>2</sup> ⋅ °C on the inner surface of the tube and  $h_o = 1200 \text{ W/m}^2 \cdot ^{\circ}\text{C}$  on the outer surface. For a fouling factor of  $R_{t,i} = 0.0004 \,\mathrm{m^2 \cdot °C/W}$  on the tube side and  $R_{t,o} = 0.0001 \,\mathrm{m^2 \cdot °C/W}$  on the shell side, determine (a) the thermal resistance of the heat exchanger per unit length and (b) the overall heat transfer coefficients,  $U_i$  and  $U_o$  based on the inner and outer surface areas of the tube, respectively.

Solution The heat transfer coefficients and the fouling factors on lube and shell side of a heat exchanger are given. The thermal resistance and the overall heat transfer coefficients based on the inner and outer areas are to be determined.

**Assumptions** The heat transfer coefficients and the fouling factors are constant and uniform.

Analysis (a) The schematic of the heat exchanger is given in Figure 10-111 Tight thermal resistance for an unfinned shell-and-tube heat exchanger with fouling of both heat transfer surfaces is given by Equation 10-8 as

$$R = \frac{1}{UA} = \frac{1}{U_i A_i} = \frac{1}{U_o A_o} = \frac{1}{h_i A_i} + \frac{R_{l,i}}{A_i} + \frac{\ln (D_o / D_i)}{2\pi k L} + \frac{R_{l,o}}{A_o} + \frac{1}{h_o A_o}$$

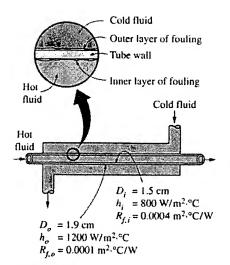
where

$$A_i = \pi D_i L = \pi (0.015 \text{ m})(1 \text{ m}) = 0.0471 \text{ m}^2$$
  
 $A_o = \pi D_o L = \pi (0.019 \text{ m})(1 \text{ m}) = 0.0597 \text{ m}^2$ 

Substituting, the total thermal resistance is determined to be

$$R = \frac{1}{(800 \text{ W/m}^2 \cdot ^\circ\text{C})(0.0471 \text{ m}^2)} + \frac{0.0004 \text{ m}^2 \cdot ^\circ\text{C/W}}{0.0471 \text{ m}^2} + \frac{\ln (0.019/0.015)}{2\pi (15.1 \text{ W/m} \cdot ^\circ\text{C})(1 \text{ m})} + \frac{0.0001 \text{ m}^2 \cdot ^\circ\text{C/W}}{0.0597 \text{ m}^2} + \frac{1}{(1200 \text{ W/m}^2 \cdot ^\circ\text{C})(0.0597 \text{ m}^2)} = (0.02654 + 0.00849 + 0.0025 + 0.00168 + 0.01396)^\circ\text{C/W} = 0.0532^\circ\text{C/W}$$

Discussion Note that about 19 percent of the total thermal resistance in the total the total the total thermal resistance in the total case is due to fouling and about 5 percent of it is due to the steel tube set the two fluids. The rest (76 percent) is due to the convection resistances continue sides of the interest in the sides of two sides of the inner tube.



**FIGURE 10-11** Schematic for Example 10-2.

h Knowing the to overall heat transfe are determined ag

$$U_o = -\frac{1}{F}$$

cussion. Note h (by 27 percent) in heat transfer surfa d negligible thick dicients would be

### 103 M ANALY

Heat exchangers: himself or hersel Specified tempera predict) the outlet calexchanger. In the follow chalysis of heat e (or LMTD) meth method for the s considerations. Heat exchang their operating Mid Properties s

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thermal resistance and the heat transfer surface areas, the right total thermal resistance and the heat transfer surface areas, the right transfer coefficient based on the inner and outer surfaces of the tube at transfer coefficient based on the inner and outer surfaces of the tube at transfer surface areas, the right total transfer surface areas, the right transfer surface areas, the

$$l = \frac{1}{RA_c} = \frac{1}{(0.0532 \text{ °C/W})(0.0471 \text{ m}^2)} = 399.1 \text{ W/m}^2 \cdot \text{°C}$$

$$\frac{1}{BA_0} = \frac{1}{(0.0532 \, ^{\circ}\text{C/W})(0.0597 \, \text{m}^2)} = 314.9 \, \text{W/m}^2 \cdot ^{\circ}\text{C}$$

Note that the two overall heat transfer coefficients differ significantly case because of the considerable difference between the interest face areas on the inner and the outer sides of the tube. For tubes in sersifications, the difference between the two overall heat transfer co-could be negligible.

## ANALYSIS OF HEAT EXCHANGERS

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changers are commonly used in practice, and an engineer often finds for herself in a position to select a heat exchanger that will achieve a lemperature change in a fluid stream of known mass flow rate, or to the fourth temperatures of the hot and cold fluid streams in a specified exchanger.

In the following sections, we will discuss the two methods used in the was of heat exchangers. Of these, the log mean temperature difference (ATD) method is best suited for the first task and the effectiveness-NTU belief the second task stated above. But first we present some general

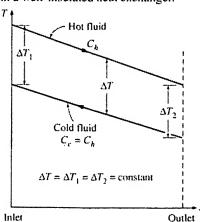
leatexchangers usually operate for long periods of time with no change their operating conditions. Therefore, they can be modeled as steady-flow the Assuch, the mass flow rate of each fluid remains constant, and the properties such as temperature and velocity at any inlet or outlet remain the sine Also, the fluid streams experience little or no change in their modes and elevations, and thus the kinetic and potential energy changes the single. The specific heat of a fluid, in general, changes with temperature range, it can be treated as a constant at heavy value with little loss in accuracy. Axial heat conduction along the is usually insignificant and can be considered negligible. Finally, the surface of the heat exchanger is assumed to be perfectly insulated, so that is no heat loss to the surrounding medium, and any heat transfer between the two fluids only.

dealizations stated above are closely approximated in practice, and really simplify the analysis of a heat exchanger with little sacrifice of therefore, they are commonly used. Under these assumptions, the of thermodynamics requires that the rate of heat transfer from third be equal to the rate of heat transfer to the cold one. That is,

Analysis of Heat Exchangers

#### **FIGURE 10-12**

Two fluids that have the same mass flow rate and the same specific heat experience the same temperature change in a well-insulated heat exchanger.



$$Q = m_c C_{pc} (T_{c, \text{out}} - T_{c, \text{in}})$$
(10.9)

and

$$Q = m_h C_{ph} (T_{h, \text{in}} - T_{h, \text{out}}) \qquad (10.10)$$

where the subscripts c and h stand for cold and hot fluids, respectively, and

$$\dot{m}_c$$
,  $\dot{m}_h$  = mass flow rates  
 $C_{pc}$ ,  $C_{ph}$  = specific heats  
 $T_{c,\text{out}}$ ,  $T_{h,\text{out}}$  = outlet temperatures  
 $T_{c,\text{in}}$ ,  $T_{h,\text{in}}$  = inlet temperatures

Note that the heat transfer rate  $\dot{Q}$  is taken to be a positive quantity, and is direction is understood to be from the hot fluid to the cold one in accordance with the second law of thermodynamics.

In heat exchanger analysis, it is often convenient to combine the product of the *mass flow rate* and the *specific heat* of a fluid into a single quantity. This quantity is called the **heat capacity rate** and is defined as

$$C = mC_p \tag{10-11}$$

The heat capacity rate of a fluid stream represents the rate of heat transfer needed to change the temperature of the fluid stream by 1°C as it flows through a heat exchanger. Note that in a heat exchanger, the fluid with a large heat capacity rate will experience a small temperature change, and the fluid with a small heat capacity rate will experience a large temperature change. Therefore, doubling the mass flow rate of a fluid while leaving everything else unchanged will halve the temperature change of that fluid.

With the definition of the heat capacity rate above, Equations 10-19 and 10-10 can also be expressed as

$$Q = C_c (T_{c, \text{out}} - T_{c, \text{in}}) \qquad (10-12)$$

and

$$\dot{Q} = C_h (T_{h, \text{in}} - T_{h, \text{out}})$$
 (10-1<sup>3</sup>)

That is, the heat transfer rate in a heat exchanger is equal to the heat cape rate of either fluid multiplied by the temperature change of that fluid that the only time the temperature rise of a cold fluid is equal to the temperature drop of the hot fluid is when the heat capacity rates of the two fluid are equal to each other (Fig. 10-12).

Two special types of heat exchangers commonly used in practice condensers and boilers. One of the fluids in a condenser or a boiler under a phase-change process, and the rate of heat transfer is expressed as

where m is the rate enthalpy of vapority. An ordinary fluid constant temper 10.13. The heat capproach infinity of  $\ell=mC_p\to\infty$  who finite quantity. The fluid is conveniently. The rate of he analogous manner

where U is the ow and  $\Delta T_m$  is an app duids. Here the su sions of the heat e and the temperatur are not constant are The average v nuned as described coefficients for eat emperature differ its determination i

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The Log Mean Temperature Difference Method

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ate of heat transfer by 1°C as it flows he fluid with a large hange, and the fluid emperature change, leaving everything fluid.

Equations 10-9 and

(10-13)

to the heat capacity; of that fluid. Note equal to the temperes of the two fluids

sed in practice are r a boiler undergoes pressed as where m is the rate of evaporation or condensation of the fluid and  $h_{fg}$  is the inhalpy of vaporization of the fluid at the specified temperature or pressure. An ordinary fluid absorbs or releases a large amount of heat essentially a constant temperature during a phase-change process, as shown in Figure 10-13. The heat capacity rate of a fluid during a phase-change process must approach infinity since the temperature change is practically zero. That is,  $c = mC_p \rightarrow \infty$  when  $\Delta T \rightarrow 0$ , so that the heat transfer rate  $\dot{Q} = mC_p \Delta T$  is a natile quantity. Therefore, in heat exchanger analysis, a condensing or boiling find is conveniently modeled as a fluid whose heat capacity rate is infinity.

The rate of heat transfer in a heat exchanger can also be expressed in an malogous manner to Newton's law of cooling as

$$\dot{Q} = UA \, \Delta T_m \tag{10-15}$$

where U is the overall heat transfer coefficient, A is the heat transfer area, and  $\Delta T_m$  is an appropriate average temperature difference between the two fulds. Here the surface area A can be determined precisely using the dimensions of the heat exchanger. However, the overall heat transfer coefficient U and the temperature difference  $\Delta T$  between the hot and cold fluids, in general, are not constant and vary along the heat exchanger.

The average value of the overall heat transfer coefficient can be determined as described in the preceding section by using the average convection coefficients for each fluid. It turns out that the appropriate form of the mean emperature difference between the two fluids is *logarithmic* in nature, and as determination is presented in the next section.

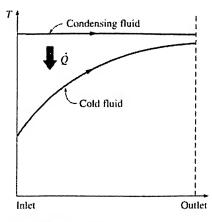


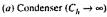
Earlier, we mentioned that the temperature difference between the hot and old fluids varies along the heat exchanger, and it is convenient to have a mean temperature difference  $\Delta T_m$  for use in the relation

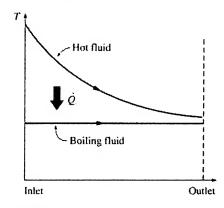
$$Q = UA\Delta T_m$$

In order to develop a relation for the equivalent average temperature difference between the two fluids, consider the parallel-flow double-pipe heat exchanger shown in Figure 10-14. Note that the temperature difference  $\Delta T$  between the hot and cold fluids is large at the inlet of the heat exchanger but decreases exponentially toward the outlet. As you would expect, the temperature of the hot fluid decreases and the temperature of the cold fluid increases along the heat exchanger, but the temperature of the cold fluid can never exceed that of the hot fluid no matter how long the heat exchanger is.

Assuming the outer surface of the heat exchanger to be well insulated so that any heat transfer occurs between the two fluids, and disregarding any thanges in kinetic and potential energy, an energy balance on each fluid in a



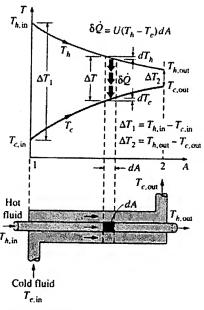




(b) Boiler  $(C_r \to \infty)$ 

#### **FIGURE 10-13**

Variation of fluid temperatures in a heat exchanger when one of the fluids condenses or boils.



**FIGURE 10-14** 

Variation of the fluid temperatures in a parallel-flow double-pipe heat exchanger.

differential section of the heat exchanger can be expressed as

$$\delta \dot{Q} = -\dot{m}_h C_{ph} dT_h \tag{10-16}$$

and

$$\delta \dot{Q} = \dot{m}_c C_{pc} dT_c \tag{10.11}$$

That is, the rate of heat loss from the hot fluid at any section of a hear exchanger is equal to the rate of heat gain by the cold fluid in that section. The temperature change of the hot fluid is a negative quantity, and so negative sign is added to Equation 10-16 to make the heat transfer rate  $Q_2$  positive quantity. Solving the equations above for  $dT_h$  and  $dT_c$  gives

$$dT_h = -\frac{\delta \dot{Q}}{\dot{m}_h C_{nh}} \tag{10.18}$$

and

$$dT_c = \frac{\delta \dot{Q}}{\dot{m}_c C_{ac}} \tag{10-19}$$

Taking their difference, we get

$$dT_h - dT_c = d(T_h - T_c) = -\delta Q \left( \frac{1}{\dot{m}_h C_{ch}} + \frac{1}{\dot{m}_c C_{cc}} \right)$$
 (10-20)

The rate of heat transfer in the differential section of the heat exchanger can also be expressed as

$$\delta Q = U(T_h - T_c)dA \tag{10.21}$$

Substituting this equation into Equation 10-20 and rearranging gives

$$\frac{d(T_h - T_c)}{T_h - T_c} = -U \, dA \left( \frac{1}{\dot{m}_h C_{oh}} + \frac{1}{\dot{m}_c C_{oc}} \right) \tag{10.22}$$

Integrating from the inlet of the heat exchanger to its outlet, we obtain

$$\ln \frac{T_{h,\text{out}} - T_{c,\text{out}}}{T_{h,\text{in}} - T_{c,\text{in}}} = -UA \left( \frac{1}{\dot{m}_b C_{ph}} + \frac{1}{\dot{m}_c C_{pc}} \right)$$
(10-23)

Finally, solving Equations 10-9 and 10-10 for  $\dot{m}_c C_{pc}$  and  $\dot{m}_h C_{ph}$  and substituting into Equation 10-23 gives, after some rearrangement,

$$\dot{Q} = UA \, \Delta T_{\rm lm} \tag{10.2}$$

where

$$\Delta T_{\text{lm}} = \frac{\Delta T_1 - \Delta T_2}{\ln \left(\Delta T_1 / \Delta T_2\right)}.$$

is the log mean temperature difference, which is the suitable form of the average temperature difference for use in the analysis of heat exchanges. Here  $\Delta T_1$  and  $\Delta T_2$  represent the temperature difference between the two fluids

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## Counter-Flow

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itable form of the f heat exchangers ween the two fluids the two ends (inlet and outlet) of the heat exchanger. It makes no difference the two ends (inlet and outlet) of the heat exchanger is designated as the *inlet* or the *outlet* [19, 10-15].

The temperature difference between the two fluids decreases from  $\Delta T_1$  the inlet to  $\Delta T_2$  at the outlet. Thus, it is tempting to use the arithmetic mean temperature  $\Delta T_{\rm am} = \frac{1}{2}(\Delta T_1 + \Delta T_2)$  as the average temperature difference. The logarithmic mean temperature difference  $\Delta T_{\rm lm}$  is obtained by tracing the actual temperature profile of the fluids along the heat exchanger and san exact representation of the average temperature difference between the local fluids. It truly reflects the exponential decay of the local temperature difference.

Note that  $\Delta T_{\rm lm}$  is always less than  $\Delta T_{\rm am}$ . Therefore, using  $\Delta T_{\rm am}$  in calculations instead of  $\Delta T_{\rm lm}$  will overestimate the rate of heat transfer in a heat exchanger between the two fluids. When  $\Delta T_1$  differs from  $\Delta T_2$  by no more than 40 percent, the error in using the arithmetic mean temperature difference is less than 1 percent. But the error increases to undesirable levels when  $\Delta T_1$  differs from  $\Delta T_2$  by greater amounts. Therefore, we should always use the logarithmic mean temperature difference when determining the rate of heat transfer in a heat exchanger.

#### **Counter-Flow Heat Exchangers**

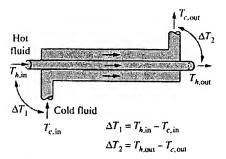
The variation of temperatures of hot and cold fluids in a counter-flow heat exchanger is given in Figure 10-16. Note that the hot and cold fluids enter the heat exchanger from opposite ends, and the outlet temperature of the cold fluid in this case may exceed the outlet temperature of the hot fluid. In the limiting case, the cold fluid will be heated to the inlet temperature of the hot fluid. However, the outlet temperature of the cold fluid can never exceed the inlet temperature of the hot fluid, since this would be a violation of the second law of thermodynamics.

The relation above for the log mean temperature difference is developed using a parallel-flow heat exchanger, but we can show by repeating the analysis above for a counter-flow heat exchanger that is also applicable to counterflow heat exchangers. But this time,  $\Delta T_1$  and  $\Delta T_2$  are expressed as shown in Figure 10-15.

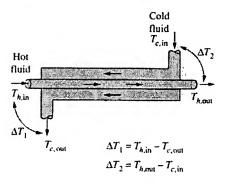
For specified inlet and outlet temperatures, the log mean temperature difference for a counter-flow heat exchanger is always greater than that for a parallel-flow heat exchanger. That is,  $\Delta T_{\text{Im},CF} > \Delta T_{\text{Im},PF}$ , and thus a smaller surface area (and thus a smaller heat exchanger) is needed to achieve a specified heat transfer rate in a counter-flow heat exchanger. Therefore, it is common practice to use counter-flow arrangements in heat exchangers.

In a counter-flow heat exchanger, the temperature difference between the hot and the cold fluids will remain constant along the heat exchanger when the heat capacity rates of the two fluids are equal (that is,  $\Delta T = \text{constant}$  when  $C_h = C_c$  or  $\dot{m}_h C_{ph} = \dot{m}_c C_{pc}$ ). Then we have  $\Delta T_1 = \Delta T_2$ , and the log mean temperature difference relation above gives  $\Delta T_{lm} = \frac{0}{0}$ , which is indeterminate. It can be shown by the application of l'Hôpital's rule that in this case we have  $\Delta T_{lm} = \Delta T_1 = \Delta T_2$ , as expected.

The Log Mean Temperature Difference Method



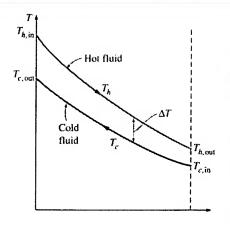
(a) Parallel-flow heat exchangers

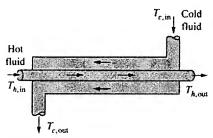


(b) Counter-flow heat exchangers

#### FIGURE 10-15

The  $\Delta T_1$  and  $\Delta T_2$  expressions in parallel-flow and counter-flow heat exchangers.



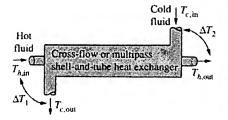


#### **FIGURE 10-16**

The variation of the fluid temperatures in a counter-flow double-pipe heat exchanger.

#### **FIGURE 10-17**

The determination of the heat transfer rate for cross-flow and multipass shell-and-tube heat exchangers using the correction factor.



Heat transfer rate:

where 
$$\dot{Q} = UAF \Delta T_{lm,CF}$$

$$\Delta T_{lm,CF} = \frac{\Delta T_1 - \Delta T_2}{\ln(\Delta T_1/\Delta T_2)}$$

$$\Delta T_1 = T_{h,\text{in}} - T_{c,\text{out}}$$

$$\Delta T_2 = T_{h,\text{out}} - T_{c,\text{in}}$$

F = ... (Fig. 10–18)

A condenser or a boiler can be considered to be either a paralla counter-flow heat exchanger since both approaches give the same result.

## Multipass and Cross-Flow Heat Exchangers: Use of a Correction Factor

The log mean temperature difference  $\Delta T_{\rm lm}$  relation developed earlier ited to parallel-flow and counter-flow heat exchangers only. Similar relations are also developed for *cross-flow* and *multipass shell-and-tube* heat exchangers, but the resulting expressions are too complicated because of the complete conditions.

In such cases, it is convenient to relate the equivalent temperature difference to the log mean temperature difference relation for the counter-now as

$$\Delta T_{\rm lm} = F \Delta T_{\rm lm,CF} \tag{0}$$

where F is the correction factor, which depends on the geometry of the line exchanger and the inlet and outlet temperatures of the hot and coldinal streams. The  $\Delta T_{\text{Im},CF}$  is the log mean temperature difference for the case counter-flow heat exchanger with the same inlet and outlet temperatures is determined from Equation 10-25 by taking  $\Delta T_1 = T_{h,\text{in}} - T_{c,\text{out}}$  and  $\Delta T_{h,\text{out}} - T_{c,\text{in}}$  (Fig. 10-17).

The correction factor is less than unity for a cross-flow and mulips shell-and-tube heat exchanger. That is,  $F \le 1$ . The limiting value of F corresponds to the counter-flow heat exchanger. Thus, the correction factor F for a heat exchanger is a measure of deviation of the  $\Delta T_{\rm lm}$  from the approximate sponding values for the counter-flow case.

The correction factor F for common cross-flow and shell-and-tube hear exchanger configurations is given in Figure 10-18 versus two temperature ratios P and R defined as

$$P = \frac{i_2 - i_1}{T_1 - i_1}$$
 (00)

and

$$R = \frac{T_1 - T_2}{T_1 - T_2} = \frac{(mC_p)_{\text{tube side}}}{(mC_p)}$$

where the subscripts 1 and 2 represent the *inlet* and *outlet*, respectively that for a shell-and-tube heat exchanger, T and t represent the *shell-andality* side temperatures, respectively, as shown in the correction factor characteristic makes no difference whether the hot or the cold fluid flows through the side or the tube. The determination of the correction factor F requires the ability of the *inlet* and the *outlet* temperatures for both the cold and hounded.

Note that the value of P ranges from 0 to 1. The value of R, on the chand, ranges from 0 to infinity, with R = 0 corresponding to the phase-change (condensation or boiling) on the shell-side and  $R \to \infty$  to phase-change R

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The Log Mean Temperature Difference Method

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0.6

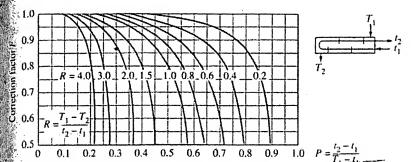
metry of the hear and cold fluid for the case of a emperatures and  $T_{c, \text{out}}$  and  $\Delta T_2 =$ 

w and multipass g value of F = 1correction factor n from the corre-

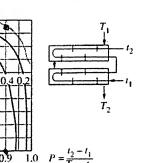
ell-and-tube heat two temperature

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respectively. Note e shell- and tube 1 factor charts. If through the shell equires the availold and hot fluids of R, on the other the phase-change phase-change on



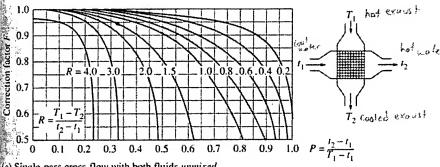
(a) One-shell pass and 2, 4, 6, etc. (any multiple of 2), tube passes



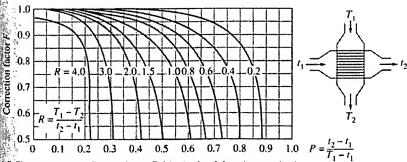
(b) Two-shell passes and 4, 8, 12, etc. (any multiple of 4), tube passes

0.4 0.5 0.6 0.7

0.3



(c) Single-pass cross-flow with both fluids unmixed



(d) Single-pass cross-flow with one fluid mixed and the other unmixed

FIGURE 10-18

Correction factor F charts for common shell-and-tube and cross-flow heat exchangers (from Bowman, Mueller, and Nagle, Ref. 2).

Steam
30°C

Cooling water
14°C

22°C

FIGURE 10-19
Schematic for Example 10-3.

the tube side. The correction factor is F = 1 for both of these limiting. Therefore, the correction factor for a *condenser* or *boiler* is F = 1, regard of the configuration of the heat exchanger.

#### **EXAMPLE 10-3** The Condensation of Steam in a Condenser

Steam in the condenser of a steam power plant is to be condensed at a temperature of 30°C with cooling water from a nearby lake, which enters the tubes of the condenser at 14°C and leaves at 22°C. The surface area of the tubes is 45 m and the overall heat transfer coefficient is 2100 W/m²·°C. Determine the nation of the cooling water needed and the rate of condensation of the season the condenser.

**Solution** Steam is condensed by cooling water in the condenser of a plant. The mass flow rate of the cooling water and the rate of condensation are be determined.

Assumptions 1 Steady operating conditions exist. 2 The heat exchager is well insulated so that heat loss to the surroundings is negligible and thus heat transfer from the hot fluid is equal to the heat transfer to the cold fluid. 3 Changes in the kinetic and potential energies of fluid streams are negligible. 4 There is no found 5 Fluid properties are constant.

Properties The heat of vaporization of water at 30°C is  $h_{\rm ig} = 2431$  kJ and the specific heat of cold water at the average temperature of 18°C is  $C_{\rm p} = 4184$  J/kg.°C (Table A-9).

Analysis The schematic of the condenser is given in Figure 10-19. The condenser can be treated as a counter-flow heat exchanger since the temperature of one of the fluids (the steam) remains constant.

The temperature difference between the steam and the cooling water at two ends of the condenser is

$$\Delta T_1 = T_{h,\text{in}} - T_{c,\text{out}} = (30 - 22)^{\circ}\text{C} = 8^{\circ}\text{C}$$
  
 $\Delta T_2 = T_{h,\text{out}} - T_{c,\text{in}} = (30 - 14)^{\circ}\text{C} = 16^{\circ}\text{C}$ 

That is, the temperature difference between the two fluids varies from 8°C at 0°1 end to 16°C at the other. The proper average temperature difference between two fluids is the *logarithmic mean temperature difference* (not the arithmeter which is determined from

$$\Delta T_{lm} = \frac{\Delta T_1 - \Delta T_2}{\ln (\Delta T_1 / \Delta T_2)} = \frac{8 - 16}{\ln (8/16)} = 11.5$$
°C

This is a little less than the arithmetic mean temperature difference  $\frac{1}{2}(8 + 16) = 12^{\circ}$ C. Then the heat transfer rate in the condenser is determined in

$$Q = UA\Delta T_{im} = (2100 \text{ W/m}^2 \cdot ^{\circ}\text{C})(45 \text{ m}^2)(11.5^{\circ}\text{C}) = 1,086,750 \text{ W}$$

Therefore, the steam will lose heat at a rate of 1,086.75 kW as it flows through condenser, and the cooling water will gain practically all of it, since the condense well insulated.

The mass flow rate of the cooling water and the rate of the condensation the steam are determined from  $\dot{O} = [\dot{m}C(T_{\text{out}} - T_{\text{in}})]_{\text{cooling water}} = (\dot{m}h_{\text{in}})_{\text{det}}$ 

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counter-flow doubleine of 1.2 kg/s. The I in al 160°C at a mass dameter of 1.5 cm. If \$40W/m² · °C, detern the desired heating.

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The Log Mean Temperature Difference Method

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it flows through the

he condensation of = (mh/s)  $\dot{m}_{\text{cooling water}} = \frac{\dot{Q}}{C_p(T_{\text{out}} - T_{\text{in}})}$   $= \frac{1,086.75 \text{ kJ/s}}{(4.184 \text{ kJ/kg} \cdot ^{\circ}\text{C})(22 - 14)^{\circ}\text{C}} = 32.5 \text{ kg/s}$ 

$$\dot{m}_{\text{steam}} = \frac{\dot{Q}}{h_{fg}} = \frac{1,086.75 \text{ kJ/s}}{2431 \text{ kJ/kg}} = 0.45 \text{ kg/s}$$

therefore, we need to circulate about 72 kg of cooling water for each 1 kg of condensing to remove the heat released during the condensation process.

#### EXAMPLE 10-4 Heating Water in a Counter-Flow Heat Exchanger

A counter-flow double-pipe heat exchanger is to heat water from 20°C to 80°C at a tale of 1.2 kg/s. The heating is to be accomplished by geothermal water available at 160°C at a mass flow rate of 2 kg/s. The inner tube is thin-walled and has adiameter of 1.5 cm. If the overall heat transfer coefficient of the heat exchanger 3640 W/m² · °C, determine the length of the heat exchanger required to achieve the desired heating.

Solution Water is heated in a counter-flow double-pipe heat exchanger by gethermal water. The required length of the heat exchanger is to be determined.

assumptions 1 Steady operating conditions exist. 2 The heat exchanger is well insulated so that heat loss to the surroundings is negligible and thus heat transfer from the hot fluid is equal to the heat transfer to the cold fluid. 3 Changes in the treat and potential energies of fluid streams are negligible. 4 There is no fouling. 1 Fluid properties are constant.

Properties: We take the specific heats of water and geothermal fluid to be 4.18 and 4.31 kJ/kg.°C, respectively.

Analysis. The schematic of the heat exchanger is given in Figure 10-20. The rate of heat transfer in the heat exchanger can be determined from

$$Q = [mC_{\rho}(T_{\text{out}} - T_{\text{in}})]_{\text{water}} = (1.2 \text{ kg/s})(4.18 \text{ kJ/kg} \cdot ^{\circ}\text{C})(80 - 20)^{\circ}\text{C} = 301.0 \text{ kW}$$

Noting that all of this heat is supplied by the geothermal water, the outlet temperature of the geothermal water is determined to be

$$T_{\text{out}} = T_{\text{in}} - \frac{\dot{Q}}{mC_p}$$

$$= 160^{\circ}\text{C} - \frac{301.0 \text{ kW}}{(2 \text{ kg/s})(4.31 \text{ kJ/kg} \cdot ^{\circ}\text{C})}$$

$$= 125.1^{\circ}\text{C}$$

howing the inlet and outlet temperatures of both fluids, the logarithmic mean emperature difference for this counter-flow heat exchanger becomes

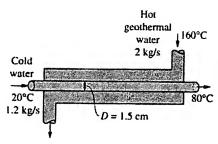


FIGURE 10-20 Schematic for Example 10-4.

$$\Delta T_1 = T_{h,\text{in}} - T_{c,\text{out}} = (160 - 80)^{\circ}\text{C} = 80^{\circ}\text{C}$$
  
 $\Delta T_2 = T_{h,\text{out}} - T_{c,\text{in}} = (125.1 - 20)^{\circ}\text{C} = 105.1^{\circ}\text{C}$ 

and

$$\Delta T_{\rm im} = \frac{\Delta T_1 - \Delta T_2}{\ln (\Delta T_1 / \Delta T_2)} = \frac{80 - 105.1}{\ln (80 / 105.1)} = 92.0^{\circ}\text{C}$$

Then the surface area of the heat exchanger is determined to be

$$\dot{O} = UA \Delta T_{lm} \longrightarrow A = \frac{\dot{O}}{U\Delta T_{lm}} = \frac{301,000 \text{ W}}{(640 \text{ W/m}^2 \cdot ^{\circ}\text{C})(92.0^{\circ}\text{C})} = 5.11 \text{ m}^2$$

To provide this much heat transfer surface area, the length of the tube must be

$$A = \pi DL$$
  $\longrightarrow$   $L = \frac{A}{\pi D} = \frac{5.11 \text{ m}^2}{\pi (0.015 \text{ m})} = 108.4 \text{ m}$ 

Discussion The inner tube of this counter-flow heat exchanger (and thus the heat exchanger itself) needs to be over 100 m long to achieve the desired heat transfer, which is impractical. In cases like this, we need to use a plate heat exchanger or a multipass shell-and-tube heat exchanger with multiple passes of tube bundles.

## EXAMPLE 10-5 Heating of Glycerin in a Multipass Heat Exchanger

A 2-shell passes and 4-tube passes heat exchanger is used to heat glycerin from 20°C to 50°C by hot water, which enters the thin-walled 2-cm-diameter tubes a 80°C and leaves at 40°C (Fig. 10-21). The total length of the tubes in the heat exchanger is 60 m. The convection heat transfer coefficient is 25 W/m<sup>2</sup>·°C or the glycerin (shell) side and 160 W/m<sup>2</sup>·°C on the water (tube) side. Determine the rate of heat transfer in the heat exchanger (a) before any fouling occurs and (b) after fouling with a fouling factor of 0.0006 m<sup>2</sup>·°C/W occurs on the outer surfaces of the tubes.

**Solution** Glycerin is heated in a 2-shell passes and 4-tube passes heater changer by hot water. The rate of heat transfer for the cases of fouling and no fouling are to be determined.

Assumptions 1 Steady operating conditions exist. 2 The heat exchanger is we insulated so that heat loss to the surroundings is negligible and thus heat transfer from the hot fluid is equal to heat transfer to the cold fluid. 3 Changes in the kinetic and potential energies of fluid streams are negligible. 4 Heat transfer coefficients and fouling factors are constant and uniform. 5 The thermal resistance of the inner tube is negligible since the tube is thin-walled and highly conductive.

Analysis The tubes are said to be thin-walled, and thus it is reasonable to assume the inner surface area of the tubes to be equal to the outer surface area. Then the heat transfer surface area of this heat exchanger becomes

$$A = \pi DL = \pi (0.02 \text{ m})(60 \text{ m}) = 3.77 \text{ m}^2$$

The rate of heat transfer in this heat exchanger can be determined from

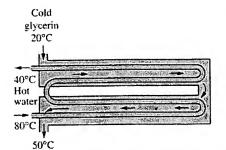


FIGURE 10-21

Schematic for Example 10-5.

 $\dot{Q} = UAF \Delta T_{im, CE}$ 

where F is the correction factor and  $\Delta T_{\rm Im,\,CF}$  is the log mean temperature difference for the counter-flow arrangement. These two quantities are determined from

The Log Mean Temperature Difference Method

$$\Delta T_1 = T_{p, in} - T_{q, out} = (80 - 50)^{\circ}C = 30^{\circ}C$$

$$\Delta T_2 = T_{h, \text{Old}} - T_{c, \text{in}} = (40 - 20)^{\circ}\text{C} = 20^{\circ}\text{C}$$

$$\Delta T_{\text{im, CF}} = \frac{\Delta T_1 - \Delta T_2}{\ln (\Delta T_1 / \Delta T_2)} = \frac{30 - 20}{\ln (30/20)} = 24.7^{\circ}\text{C}$$

and

$$P = \frac{t_2 - t_1}{T_1 - t_1} = \frac{40 - 80}{20 - 80} = 0.67$$

$$R = \frac{T_1 - T_2}{t_2 - t_1} = \frac{20 - 50}{40 - 80} = 0.75$$

$$F = 0.91$$
 (Fig. 10-18b)

(a) in the case of no fouling, the overall heat transfer coefficient U is determined

$$U = \frac{1}{\frac{1}{h_i} + \frac{1}{h_o}} = \frac{1}{\frac{1}{160 \text{ W/m}^2 \cdot ^{\circ}\text{C}}} + \frac{1}{25 \text{ W/m}^2 \cdot ^{\circ}\text{C}} = 21.6 \text{ W/m}^2 \cdot ^{\circ}\text{C}$$

Then the rate of heat transfer becomes

$$O = UAF \Delta T_{\text{im, CF}} = (21.6 \text{ W/m}^2 \cdot ^{\circ}\text{C})(3.77\text{m}^2)(0.91)(24.7^{\circ}\text{C}) = 1730\text{-W}$$

(b) When there is fouling on one of the surfaces, the overall heat transfer coefficient Uis determined from

$$U = \frac{1}{\frac{1}{h_i} + \frac{1}{h_o} + R_t} = \frac{1}{\frac{1}{160 \text{ W/m}^2 \cdot ^{\circ}\text{C}} + \frac{1}{25 \text{ W/m}^2 \cdot ^{\circ}\text{C}} + 0.0006 \text{ m}^2 \cdot ^{\circ}\text{C/W}}$$

$$= 21.3 \text{ W/m}^2 \cdot ^{\circ}\text{C}$$

The rate of heat transfer in this case becomes

$$\dot{Q} = UAF\Delta T_{lm, CF} = (21.3 \text{ W/m}^2 \cdot ^{\circ}\text{C})(3.77\text{m}^2)(0.91)(24.7^{\circ}\text{C}) = 1805 \text{ W}$$

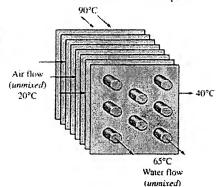
Discussion Note that the rate of heat transfer decreases as a result of fouling, as expected. The decrease is not dramatic, however, because of the relatively by convection heat transfer coefficients involved.

#### **EXAMPLE 10-6** Cooling of an Automotive Radiator

A test is conducted to determine the overall heat transfer coefficient in an automotive radiator that is a compact cross-flow water-to-air heat exchanger with both fluids (air and water) unmixed (Fig. 10-22). The radiator has 40 tubes of internal diameter 0.5 cm and length 65 cm in a closely spaced plate-finned matrix. Hot water enters the tubes at 90°C at a rate of 0.6 kg/s and leaves at 65°C. Air flows across the radiator through the interfin spaces and is heated from 20°C 0.40°C. Determine the overall heat transfer coefficient  $U_i$  of this radiator based on the inner surface area of the tubes.

#### **FIGURE 10-22**

Schematic for Example 10-6.



tubes in the heat \$ 25 W/m<sup>2</sup> · °C on ) side. Determine

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The thermal ress walled and highly

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nined from

**Solution** During an experiment involving an automotive radiator (holding) exit temperatures of water and air and the mass flow rate of water are meant. The overall heat transfer coefficient based on the inner surface area is to determined.

Assumptions 1 Steady operating conditions exist. 2 Changes in the kinetic repotential energies of fluid streams are negligible. 3 Fluid properties are constant.

Properties The specific heat of water at the average temperature of (90 + 65)? = 77.5°C is 4.195 kJ/kg • °C.

Analysis The rate of heat transfer in this radiator from the hot water to the carry determined from an energy balance on water flow,

$$\dot{Q} = [\dot{m}C_p(T_{\text{in}} - T_{\text{out}})]_{\text{water}} = (0.6 \text{ kg/s})(4.195 \text{ kJ/kg} \cdot ^{\circ}\text{C})(90 - 65)(90$$

The tube-side heat transfer area is the total surface area of the tubes and other determined from

$$A_i = n\pi D_i L = (40)\pi (0.005 \text{ m})(0.65 \text{ m}) = 0.408 \text{ m}$$

Knowing the rate of heat transfer and the surface area, the overall heattransfer coefficient in this heat exchanger can be determined from

$$Q = U_i A_i F \Delta T_{\text{Im, }CF} \longrightarrow U_i = \frac{Q^2}{A_i F \Delta T_{\text{im, }CF}}$$

where F is the correction factor and  $\Delta T_{\text{Im, }CF}$  is the log mean temperature ence for the counter-flow arrangement. These two quantities are found to be

$$\Delta T_1 = T_{h, \text{in}} - T_{c, \text{out}} = (90 - 40)^{\circ}\text{C} = 50^{\circ}\text{C}$$
  
 $\Delta T_2 = T_{h, \text{out}} - T_{c, \text{in}} = (65 - 20)^{\circ}\text{C} = 45^{\circ}\text{C}$ 

$$\Delta T_{\text{Im, }CF} = \frac{\Delta T_1 - \Delta T_2}{\ln (\Delta T_1 / \Delta T_2)} = \frac{50 - 45}{\ln (50/45)} = 47.6^{\circ}\text{C}$$

and

$$P = \frac{t_2 - t_1}{T_1 - t_1} = \frac{65 - 90}{20 - 90} = 0.36$$

$$R = \frac{T_1 - T_2}{t_2 - t_1} = \frac{20 - 40}{65 - 90} = 0.80$$

$$F = 0.97$$
(Fig. 10-186)

Substituting, the overall heat transfer coefficient  $U_i$  is determined to  $D_i$ 

$$U_i = \frac{\dot{Q}}{A_i F \Delta T_{\text{Im, }CF}} = \frac{62,930 \text{ W}}{(0.408 \text{ m}^2)(0.97)(47.6^{\circ}\text{C})} = 3341 \text{ W/m}^{2 \text{ e} \cdot \text{C}}$$

Note that the overall heat transfer coefficient on the air side would be much because of the large surface area involved on that side.

## 10-5 & THE EFFECTIVENESS-NTU METHOD

The log mean temperature difference (LMTD) method discussed in the vious section is easy to use in heat exchanger analysis when the interest outlet temperatures of the hot and cold fluids are known or can be determined.

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ne inlet and the be determined from an energy balance. Once  $\Delta T_{\rm lm}$ , the mass flow rates, and the overall heat transfer coefficient are available, the heat transfer surface area of the heat exchanger can be determined from

 $\dot{Q} = UA \Delta T_{\rm lm}$ 

Therefore, the LMTD method is very suitable for determining the *size* of a feat exchanger to realize prescribed outlet temperatures when the mass flow and the inlet and outlet temperatures of the hot and cold fluids are recified.

with the LMTD method, the task is to select a heat exchanger that will meet the prescribed heat transfer requirements. The procedure to be followed by the selection process is as follows:

Select the type of heat exchanger suitable for the application.

2. Determine any unknown inlet or outlet temperature and the heat transfer rate using an energy balance.

Calculate the log mean temperature difference  $\Delta T_{\rm lm}$  and the correction factor F, if necessary.

Obtain (select or calculate) the value of the overall heat transfer coefficient U.

Calculate the heat transfer surface area A.

The task is completed by selecting a heat exchanger that has a heat transfer surface area equal to or larger than A.

A second kind of problem encountered in heat exchanger analysis is the determination of the heat transfer rate and the outlet temperatures of the hot and cold fluids for prescribed fluid mass flow rates and inlet temperatures when the type and size of the heat exchanger are specified. The heat transfer surface area A of the heat exchanger in this case is known, but the outlet temperatures are not. Here the task is to determine the heat transfer performance of a specified heat exchanger or to determine if a heat exchanger available in storage will do the job.

The LMTD method could still be used for this alternative problem, butthe procedure would require tedious iterations, and thus it is not practical. In an attempt to eliminate the iterations from the solution of such problems. Kays and London came up with a new method in 1955 called the effectiveness-NTU method, which greatly simplified heat exchanger malysis.

This new method is based on a dimensionless parameter called the heat transfer effectiveness  $\varepsilon$ , defined as

Actual heat transfer rate

Maximum possible heat transfer rate

(10-29

The Effectiveness-NTU Method

Hot oil 130°C 40 kg/s  $C_{c} = m_{c}C_{pc} = 104.5 \text{ kW/°C}$   $C_{h} = m_{c}C_{ph} = 92 \text{ kW/°C}$   $C_{min} = 92 \text{ kW/°C}$   $\Delta T_{max} = T_{h,in} - T_{c,in} = 110°C$   $Q_{max} = C_{min} \Delta T_{max} = 10,120 \text{ kW}$ 

#### **FIGURE 10-23**

The determination of the maximum rate of heat transfer in a heat exchanger.

The actual heat transfer rate in a heat exchanger can be determined from an energy balance on the hot or cold fluids and can be expressed as

$$\dot{Q} = C_c (T_{c,\text{out}} - T_{c,\text{in}}) = C_h (T_{h,\text{in}} - T_{h,\text{out}})$$
 (10-30)

where  $C_c = \dot{m}_c C_{pc}$  and  $C_h = \dot{m}_c C_{ph}$  are the heat capacity rates of the cold and the hot fluids, respectively.

To determine the maximum possible heat transfer rate in a heat exchanger, we first recognize that the *maximum temperature difference* in a heat exchanger is the difference between the *inlet* temperatures of the hot and cold fluids. That is,



The heat transfer in a heat exchanger will reach its maximum value when (1) the cold fluid is heated to the inlet temperature of the hot fluid or (2) the hot fluid is cooled to the inlet temperature of the cold fluid. These two limiting conditions will not be reached simultaneously unless the heat capacity rates of the hot and cold fluids are identical (i.e.,  $C_c = C_h$ ). When  $C_c \neq C_h$ , which is usually the case, the fluid with the *smaller* heat capacity rate will experience a larger temperature change, and thus it will be the first to experience the maximum temperature, at which point the heat transfer will come to a halt. Therefore, the maximum possible heat transfer rate in a heat exchanger is (Fig. 10-23)



where  $C_{\min}$  is the smaller of  $C_h = \dot{m}_h C_{ph}$  and  $C_c = \dot{m}_c C_{pc}$ . This is further clarified by the following example.

#### EXAMPLE 10-7 Upper Limit for Heat Transfer in a Heat Exchanger

Cold water enters a counter-flow heat exchanger at 10°C at a rate of 8 kg/s, where it is heated by a hot water stream that enters the heat exchanger at 70°C at a rate of 2 kg/s. Assuming the specific heat of water to remain constant at  $C_p = 4.18 \, \text{kg} \cdot ^{\circ}\text{C}$ , determine the maximum heat transfer rate and the outlet temperatures of the cold and the hot water streams for this limiting case.

**Solution** Cold and hot water streams enter a heat exchanger at specified temperatures and flow rates. The maximum rate of heat transfer in the heat changer is to be determined.

Assumptions 1 Steady operating conditions exist. 2 The heat exchanger is insulated so that heat loss to the surroundings is negligible and thus heat transfer from the hot fluid is equal to heat transfer to the cold fluid. 3 Changes in the kinetic and potential energies of fluid streams are negligible. 4 Heat transfer coefficients and fouling factors are constant and uniform. 5 The thermal resistance of the inner tube is negligible since the tube is thin-walled and highly conductive.

*Properties* The specific heat of water is given to be  $C_p = 4.18 \text{ kJ/kg} \cdot ^{\circ}\text{C}$ .

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more than 60°C heated by more tures of the col

 $C_c(T_{c, \text{out}})$ 

 $\hat{Q} = C_h(T_{h, in})$ 

Discussion N perature of the maximum heat the mass flow as a result, the drop in the tem You may be limiting carolithe hot wate heat transfer in the smaller he have the sam change. This colicination

We can st water and vic mass flow rate can also show limit when the determined from an ssed as

·ut)

rates of th

rate in a heat exture difference in a atures of the houand

ximum value when ; hot fluid or Othe . These two limiting : heat capacity rates hen  $C_c \neq C_b$  which ity rate will expend e first to experience sfer will come to a in a heat exchanger

This is further

t Exchanger nger at 70°C attairate stant at  $C_p = 4.18 \text{kg}$  utlet temperatures of

hanger at specified nsfer in the heatex-

at exchanger is well nd thus heat transfer d. 3 Changes in the ble. 4 Heat transfer 5 The thermal resisn-walled and highly

.18 kJ/kg •°Ç

A schematic of the heat exchanger is given in Figure 10-24. The heat city rates of the hot and cold fluids are determined from

$$C_h = \dot{m}_h C_{ph} = (2 \text{ kg/s})(4.18 \text{ kJ/kg} \cdot ^{\circ}\text{C}) = 8.36 \text{ kW/}^{\circ}\text{C}$$

$$C_c = \dot{m_c}C_{\rho c} = (8 \text{ kg/s})(4.18 \text{ kJ/kg} \cdot ^{\circ}\text{C}) = 33.44 \text{ kW/}^{\circ}\text{C}$$

$$C_{\text{min}} = C_h = 8.36 \text{ kW/}^{\circ}\text{C}$$

s the smaller of the two heat capacity rates. Then the maximum heat ransfer rate is determined from Equation 10-32 to be

$$\dot{Q}_{\text{max}} = C_{\text{min}} (T_{h, \text{in}} - T_{c, \text{in}})$$
  
= (8.36 kW/°C)(70 - 10)°C  
= **501.6 kW**

the maximum possible heat transfer rate in this heat exchanger is 501.6 w This value would be approached in a counter-flow heat exchanger with a very heat transfer surface area.

The maximum temperature difference in this heat exchanger is  $\Delta T_{\text{max}}$  =  $T_{c,in} = (70 - 10)^{\circ}$ C = 60°C. Therefore, the hot water cannot be cooled by more than 60°C (to 10°C) in this heat exchanger, and the cold water cannot be neated by more than 60°C (to 70°C), no matter what we do. The outlet tempera-jures of the cold and the hot streams in this limiting case are determined to be

$$0 = C_c(T_{c, \text{out}} - T_{c, \text{in}}) \longrightarrow T_{c, \text{out}} = T_{c, \text{in}} + \frac{\dot{Q}}{C_c} = 10^{\circ}\text{C} + \frac{501.6 \text{ kW}}{33.44 \text{ kW/°C}} = 25^{\circ}\text{C}$$

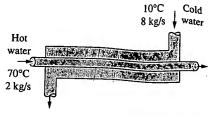
$$C_h(T_{h, \text{in}} - T_{h, \text{out}}) \longrightarrow T_{h, \text{out}} = T_{h, \text{in}} - \frac{\dot{Q}}{C_h} = 70^{\circ}\text{C} - \frac{501.6 \text{ kW}}{8.38 \text{ kW/°C}} = 10^{\circ}\text{C}$$

Discussion Note that the hot water is cooled to the limit of 10°C (the inlet temperature of the cold water stream), but the cold water is heated to 25°C only when maximum heat transfer occurs in the heat exchanger. This is not surprising, since the mass flow rate of the hot water is only one-fourth that of the cold water, and, asaresult, the temperature of the cold water increases by 0.25°C for each 1°C dropin the temperature of the hot water.

 $\sum_{i=1}^{\infty}$ ou may be tempted to think that the cold water should be heated to 70°C in helimiting case of maximum heat transfer. But this will require the temperature of the hot water to drop to -170°C (below 10°C), which is impossible. Therefore, beattransfer in a heat exchanger reaches its maximum value when the fluid with maller heat capacity rate (or the smaller mass flow rate when both fluids have the same specific heat value) experiences the maximum temperature change. This example explains why we use  $\mathcal{C}_{\mathsf{min}}$  in the evaluation of  $\mathcal{Q}_{\mathsf{max}}$  instead

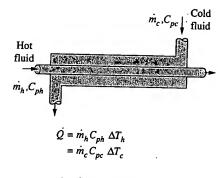
We can show that the hot water will leave at the inlet temperature of the cold water and vice versa in the limiting case of maximum heat transfer when the mass flow rates of the hot and cold water streams are identical (Fig. 10-25). We can also show that the outlet temperature of the cold water will reach the 70°C when the mass flow rate of the hot water is greater than that of the cold water.





**FIGURE 10-24** 

Schematic for Example 10-7.



$$\text{If} \quad \dot{m}_c \, C_{pc} = \dot{m}_h \, C_{ph}$$

then 
$$\Delta T_h = \Delta T_c$$

#### FIGURE 10-25

The temperature rise of the cold fluid in a heat exchanger will be equal to the temperature drop of the hot fluid when the mass flow rates and the specific heats of the hot and cold fluids are identical.

The determination of  $\dot{Q}_{max}$  requires the availability of the *inlet temperature* of the hot and cold fluids and their mass flow rates, which are usually specified. Then, once the effectiveness of the heat exchanger is known in actual heat transfer rate  $\dot{Q}$  can be determined from

 $Q = cQ_{
m max} = cC_{
m orb}(T_{
m hym} - T_{
m orb})$  (10-3)

Therefore, the effectiveness of a heat exchanger enables us to determine the heat transfer rate without knowing the *outlet temperatures* of the fluids.

The effectiveness of a heat exchanger depends on the geometry of the heat exchanger as well as the flow arrangement. Therefore, different types of heat exchangers have different effectiveness relations. Below we illustrate the development of the effectiveness  $\varepsilon$  relation for the double-pipe parallel flow heat exchanger.

Equation 10-23 developed in the previous section for a parallel-flow heat exchanger can be rearranged as

$$\ln \frac{T_{h,\text{out}} - T_{c,\text{out}}}{T_{h,\text{in}} - T_{c,\text{in}}} = -\frac{UA}{C_c} \left( 1 + \frac{C_c}{C_h} \right) \tag{10-34}$$

Also, solving Equation 10-30 for  $T_{h, out}$  gives

$$T_{h,\text{out}} = T_{h,\text{in}} - \frac{C_c}{C_h} (T_{c,\text{out}} - T_{c,\text{in}})$$
 (1035)

Substituting this relation into Equation 10-34 after adding and subtracting  $T_{c,\text{in}}$  gives

$$\ln \frac{T_{h,in} - T_{c,in} + T_{c,in} - T_{c,out} - \frac{C_c}{C_h} (T_{c,out} - T_{c,in})}{T_{h,in} - T_{c,in}} = -\frac{UA}{C_c} \left(1 + \frac{C_c}{C_h}\right)$$

which simplifies to

$$\ln\left[1 - \left(1 + \frac{C_c}{C_h}\right) \frac{T_{c,\text{out}} - T_{c,\text{in}}}{T_{h,\text{in}} - T_{c,\text{in}}}\right] = -\frac{UA}{C_c} \left(1 + \frac{C_c}{C_h}\right) \quad (1050)$$

We now manipulate the definition of effectiveness to obtain

$$\varepsilon = \frac{\dot{Q}}{\dot{Q}_{\text{max}}} = \frac{C_c (T_{c, \text{out}} - T_{c, \text{in}})}{C_{\text{min}} (T_{h, \text{in}} - T_{c, \text{in}})} \longrightarrow \frac{T_{c, \text{out}} - T_{c, \text{in}}}{T_{h, \text{in}} - T_{c, \text{in}}} = \varepsilon \frac{C_{\text{min}}}{C_c}$$

Substituting this result into Equation 10-36 and solving for  $\varepsilon$  gives the following relation for the effectiveness of a parallel-flow heat exchanger:

$$\varepsilon_{\text{parallel flow}} = \frac{1 - \exp\left[-\frac{UA}{C_c}\left(1 + \frac{C_c}{C_h}\right)\right]}{\left(1 + \frac{C_c}{C_h}\right)\frac{C_{\min}}{C_c}}$$

Thingefiner  $C_c$  c relation above can

Again G<sub>min</sub> is the itmakes no differ Effectiveness mensionless grou units NTU and is

where U is the c surface area of t Therefore, for sp of the heat transf heat exchanger.

Inheat excha

licanbe shown to

ε = fu

Effectiveness rel changers, and the common types of extensive effective extensive effective dashed lines in mixed, and the for the effective errors in charts: puterized design We make the charts given abo

The value of with NTU for s larger values.



is to determine the of the fluids. e geometry of the , different types of ow we illustrate the -pipe parallel flow

a parallel-flowheat

(10-33)

ng and subtracting

$$-\frac{UA}{C_c}\left(1+\frac{C_c}{C_c}\right)$$

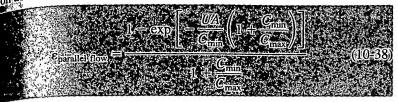
$$1 + \frac{C_c}{C_h}$$
 (10-36)

in

$$\frac{c, \text{in}}{c, \text{in}} = \epsilon \frac{C_{\text{min}}}{C_{\text{c}}};$$

ε gives the followchanger:

either  $C_c$  or  $C_h$  to be  $C_{\min}$  (both approaches give the same result), the approaches grant approaches grant approaches grant above can be expressed more conveniently as



 $C_{\min}^{2}$  is the smaller heat capacity ratio and  $C_{\max}$  is the larger one, and makes no difference whether  $C_{\min}$  belongs to the hot or cold fluid.

Effectiveness relations of the heat exchangers typically involve the diinteriorless group UA/C<sub>min</sub>. This quantity is called the number of transfer mis NTU and is expressed as

$$\underline{NTU} = \frac{\overline{UA}}{\overline{C_{\min}}} = \frac{\overline{UA}}{(\overline{m}\overline{C_p})_{\min}}, \qquad (10-39)$$

 $U_{is}$  the overall heat transfer coefficient and A is the heat transfer mace area of the heat exchanger. Note that NTU is proportional to A. therefore, for specified values of U and  $C_{\min}$ , the value of NTU is a measure The heat transfer surface area A. Thus, the larger the NTU, the larger the heat exchanger.

In heat exchanger analysis, it is also convenient to define another dimengonless quantity called capacity ratio C as



fican be shown that the effectiveness of a heat exchanger is a function of the number of transfer units NTU and the capacity ratio C. That is,

$$\varepsilon = \text{function}(UA/C_{\min}, C_{\min}/C_{\max}) = \text{function}(NTU, C)$$

Effectiveness relations have been developed for a large number of heat exchangers, and the results are given in Table 10-4. The effectivenesses of some common types of heat exchangers are also plotted in Figure 10-26. More extensive effectiveness charts and relations are available in the literature. The dashed lines in Figure 10-26f are for the case of  $C_{\min}$  unmixed and  $C_{\max}$ mixed, and the solid lines are for the opposite case. The analytic relations othe effectiveness give more accurate results than the charts, since reading ctions in charts are unavoidable, and the relations are very suitable for compuerized design analysis of heat exchangers.

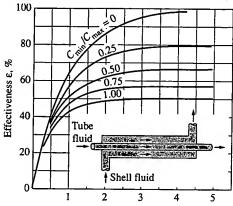
We make the following observations from the effectiveness relations and darts given above:

The value of the effectiveness ranges from 0 to 1. It increases rapidly TU for small values (up to about NTU = 1.5) but rather slowly for agen values. Therefore, the use of a heat exchanger with a large NTU ACCEPTANCE OF THE PROPERTY. The Effectiveness-

NTU Method

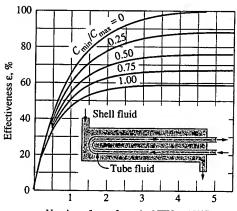
#### **FIGURE 10-26**

Effectiveness for heat exchangers (from Kays and London, Ref. 7).



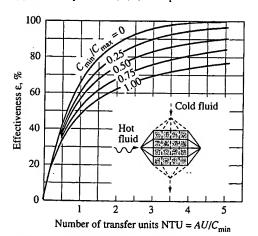
Number of transfer units NTU =  $AU/C_{min}$ 

#### (a) Parallel-flow

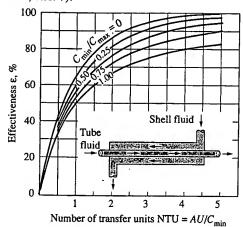


Number of transfer units NTU =  $AU/C_{min}$ 

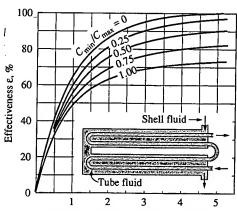
#### (c) One-shell pass and 2, 4, 6, tube passes



(e) Cross-flow with both fluids unmixed

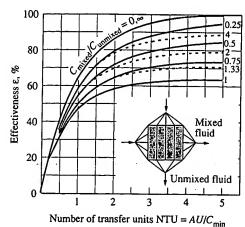


#### (b) Counter-flow



Number of transfer units NTU =  $AU/C_{min}$ 

### (d) Two-shell passes and 4, 8, 12, tube passes



(f) Cross-flow with one fluid mixed and the other unmixed

VOLISIO 4
Viectiveness relation and G = Cmin/Cmax = Tolkoxchanger

poublepipe:

Parallel flow

Counter-flow

2 Shelland tube: One-shell pass

2,4, at lube

3 Gross-flow (single-pass)

Both fluids \*

 $\mathcal{C}_{ ext{min}}$  mixed.  $\mathcal{C}_{ ext{min}}$  unmixed

 $\mathcal{C}_{\mathrm{min}}$ mixed,  $\mathcal{C}_{\mathrm{max}}$ unmixed

4 All heat exchangers with C= 0.1

Source: Kays and Lond

usually larger that dice alarge increa dicetiveness. Thus lighly desirable fr from an economica

Ror, a given N heat exchanger has flow heat exchange lowest effectivenes (Fig. 10-27).

Ine effectiven Cfor NTU values

The value of 1

Will the effective

C = 1 The case

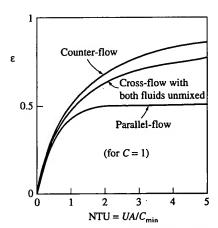
## at exchanger

Heat exchange	Effectiveness relation
Double pipe:	$\varepsilon = \frac{1 - \exp\left[-NTU(1+C)\right]}{1+C}$
Counter-flow	$\varepsilon = \frac{1 - \exp\left[-NTU(1-C)\right]}{1 - C\exp\left[-NTU(1-C)\right]}$
2 Shell and tube: One shell pass 2:4, tube passes	$\varepsilon = 2 \left\{ 1 + C + \sqrt{1 + C^2} \frac{1 + \exp\left[-NTU\sqrt{1 + C^2}\right]}{1 - \exp\left[-NTU\sqrt{1 + C^2}\right]} \right\}^{-1}$
3 Gross-flow (single-pass)	
Both fluids unmixed	$\varepsilon = 1 - \exp\left\{\frac{NTU^{0.22}}{C}[\exp\left(-CNTU^{0.78}\right) - 1]\right\}$
@ <sub>max</sub> mixed, @ <sub>min</sub> unmixed	$\varepsilon = \frac{1}{C}(1 - \exp\{1 - C[1 - \exp(-NTU)]\})$
© <sub>min</sub> mixed, © <sub>max</sub> unmixed	$\varepsilon = 1 - \exp\left\{-\frac{1}{C}[1 - \exp(-C \text{NTU})]\right\}$
A All heat exchangers with C = 0	$\varepsilon = 1 - \exp(-NTU)$

Source: Kays and London, Ref. 7.

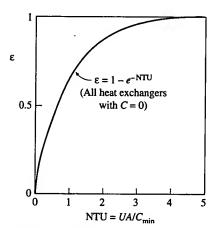
(usually larger than 3) and thus a large size cannot be justified economically, since a large increase in NTU in this case corresponds to a small increase in effectiveness. Thus, a heat exchanger with a very high effectiveness may be lighly desirable from a heat transfer point of view but rather undesirable from an economical point of view

- 2 For a given NTU and capacity ratio  $C = C_{\min}/C_{\max}$ , the counter-flow heat exchanger has the *highest* effectiveness, followed closely by the cross-flow heat exchangers with both fluids unmixed. As you might expect, the lowest effectiveness values are encountered in parallel-flow heat exchangers (Fig. 10-27).
- The effectiveness of a heat exchanger is independent of the capacity ratio of NTU values of less than about 0.3.
- The value of the capacity ratio C ranges between 0 and 1. For a given will, the effectiveness becomes a maximum for C = 0 and a minimum for C = 1. The case  $C = C_{\min}/C_{\max} \to 0$  corresponds to  $C_{\max} \to \infty$ , which is



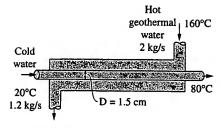
**FIGURE 10-27** 

For a specified NTU and capacity ratio C, the counter-flow heat exchanger has the highest effectiveness and the parallel-flow the lowest.



**FIGURE 10-28** 

The effectiveness relation reduces to  $\varepsilon = \varepsilon_{\text{max}} = 1 - \exp(-\text{NTU})$  for all heat exchangers when the capacity ratio C=0.



**FIGURE 10-29** 

Schematic for Example 10-8.

realized during a phase-change process in a condenser or boiler. All effective tiveness relations in this case reduce to

 $=1-\exp(-NTU)$ 

regardless of the type of heat exchanger (Fig. 10-28). Note that the temperature ture of the condensing or boiling fluid remains constant in this case. The effectiveness is the *lowest* in the other limiting case of  $C = C_{\min}/C_{\max}$ which is realized when the heat capacity rates of the two fluids are equal

Once the quantities  $C = C_{\min}/C_{\max}$  and NTU =  $UA/C_{\min}$  have been evaluated, the effectiveness  $\varepsilon$  can be determined from either the charts of (preferably) the effectiveness relation for the specified type of heat exchanger Then the rate of heat transfer  $\dot{Q}$  and the outlet temperatures  $T_{h,\text{out}}$  and  $T_{c}$ can be determined from Equations 10-33 and 10-30, respectively. Note that the analysis of heat exchangers with unknown outlet temperatures is a straightforward matter with the effectiveness-NTU method but requires rather tedious iterations with the LMTD method.

We mentioned earlier that when all the inlet and outlet temperatures are specified, the size of the heat exchanger can easily be determined using the LMTD method. Alternatively, it can also be determined from the effective ness-NTU method by first evaluating the effectiveness  $\varepsilon$  from its definite tion (Eq. 10-29) and then the NTU from the appropriate NTU relation in Table 10-5.

Note that the relations in Table 10-5 are equivalent to those in Table 1 4. Both sets of relations are given for convenience. The relations in Table. 10-4 give the effectiveness directly when NTU is known, and the relations in Table 10-5 give the NTU directly when the effectiveness  $\varepsilon$  is known.

#### **EXAMPLE 10-8** Using the Effectiveness-NTU Method

Repeat Example 10-4, which was solved with the LMTD method, using the example 10-4. fectiveness-NTU method.

Solution The schematic of the heat exchanger is redrawn in Figure 10-29 and the same assumptions are utilized.

Analysis In the effectiveness-NTU method, we first determine the heat capacity rates of the hot and cold fluids and identify the smaller one:

$$C_h = \dot{m}_h C_{ph} = (2 \text{ kg/s})(4.31 \text{ kJ/kg} \cdot ^{\circ}\text{C}) = 8.62 \text{ kW/}^{\circ}\text{C}$$
  
 $C_c = \dot{m}_c C_{pc} = (1.2 \text{ kg/s})(4.18 \text{ kJ/kg} \cdot ^{\circ}\text{C}) = 5.02 \text{ kW/}^{\circ}\text{C}$ 

Therefore,

$$C_{\text{min}} = C_c = 5.02 \text{ kW/°C}$$

and

$$C = C_{\min}/C_{\max} = 5.02/8.62 = 0.583$$

Then the maximum heat transfer rate is determined from Equation 10-32 to be

$$\dot{Q}_{\text{max}} = C_{\text{min}}(T_{h, \text{in}} - T_{c, \text{in}})$$
  
= (5.02 kW/°C)(160 - 20)°C  
= 702.8 kW

TABLE 10-5

NTU relations 1 and  $C = C_{\min}/C$ Heat exchan

1 Double-pipe:

Parallel-flow

Counter-flow

2 Shell and tub One-shell pa 2,4,... tube

3 Cross-flow(s  $\mathcal{C}_{\mathsf{max}}$  mixed,  $\mathcal{C}_{\mathsf{min}}$  unmixec

 $C_{\min}$  mixed,  $\mathcal{C}_{\mathsf{max}}$  unmixed 4 All heat exch

with C = 0Source: Kays and

that is, the m 702:8 kW. The :

 $Q = [mC_p(T_o)]$ thus, the effec

Knowing the e determined fro choose the latt

then the heat

NTU =

oprovide this

**NTU Method** 

relations for heat exchangers NTU =  $UA/C_{min}$  $C = C_{\min}/C_{\max} = (\dot{m}C_p)_{\min}/(\dot{m}C_p)_{\max}$ 

eat exchanger type	14 1 O Telation
Double-pipe:	
Parallel-flow	$NTU = -\frac{\ln[1 - \varepsilon(1 + C)]}{1 + C}$
Counter-flow	$NTU = \frac{1}{C-1} In \bigg( \frac{\varepsilon - 1}{\varepsilon C - 1} \bigg)$
Shell and tube:	

Shell and tube:

One-shell pass
$$24 \frac{1}{2} \dots \text{ tube passes}$$

$$3 \frac{C}{C} \frac{C}{C} \frac{C}{C} \frac{1}{C} - \frac{1}{C} \frac{C}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac{C}{C} \frac{C}{C} \frac{1}{C} \frac{C}{C} \frac$$

$$0.01$$
 heat exchangers  $V_{\text{T}} = V_{\text{T}} = V_{\text{T}}$ 

Source: Kays and London, Ref. 7.

@unmixed

is; the maximum possible heat transfer rate in this heat exchanger is 7028 kW. The actual rate of heat transfer in the heat exchanger is

$$(I_{\text{out}} = I_{\text{in}})_{\text{out}} - I_{\text{in}})_{\text{water}} = (1.2 \text{ kg/s})(4.18 \text{ kJ/kg} \cdot ^{\circ}\text{C})(80 - 20)^{\circ}\text{C} = 301.0 \text{ kW}$$

hus the effectiveness of the heat exchanger is

$$\varepsilon = \frac{Q}{Q_{\text{max}}} = \frac{301.0 \text{ kW}}{702.8 \text{ kW}} = 0.428$$

knowing the effectiveness, the NTU of this counter-flow heat exchanger can be determined from Figure 10-26b or the appropriate relation from Table 10-5. We choose the latter approach for greater accuracy:

$$\prod_{i=1}^{NT} \bigcup_{i=1}^{NT} \left( \frac{\varepsilon - 1}{\varepsilon C - 1} \right) = \frac{1}{0.583 - 1} \ln \left( \frac{0.428 - 1}{0.428 \times 0.583 - 1} \right) = 0.651$$

hen the heat transfer surface area becomes

$$NTU = \frac{UA}{C_{min}} \longrightarrow A = \frac{NTUC_{min}}{U} = \frac{(0.651)(5020 \text{ W/°C})}{640 \text{ W/m}^2 \cdot \text{°C}} = 5.11 \text{ m}^2$$

bprovide this much heat transfer surface area, the length of the tube must be

$$A = \pi DL \longrightarrow L = \frac{A}{\pi D} = \frac{5.11 \text{ m}^2}{\pi (0.015 \text{ m})} = 108.4 \text{ m}$$

that the tempera-in this case. The ids are equal VCmin have been her the chargor of heat exchanger. es  $T_{h, \text{out}}$  and  $T_{c}$ ctively. Note that

: temperatures are ermined using the om the effectives from its defini-

emperatures is a

hod but requires

: NTU relation in those in Table 10-

relations in Table nd the relations in is known.

thod, using the el-

n Figure 10

e the heat capacity

ation 10-3

CHAPTER 10 Heat Exchangers Discussion Note that we obtained the same result with the effectiveness-Nimmethod in a systematic and straightforward manner.

## EXAMPLE 10-9 Cooling Hot Oil by Water in a Multipass Heat Exchanger

Hot oil is to be cooled by water in a 1-shell-pass and 8-tube-passes heat exchanger. The tubes are thin-walled and are made of copper with an internal diameter of 1.4 cm. The length of each tube pass in the heat exchanger is 5 m and the overall heat transfer coefficient is 310 W/m²·°C. Water flows through the tubes at a rate of 0.2 kg/s, and the oil through the shell at a rate of 0.3 kg/s. The water and the oil enter at temperatures of 20°C and 150°C, respectively. Determine the rate of heat transfer in the heat exchanger and the outlet temperatures of the water and the oil.

**Solution** Hot oil is to be cooled by water in a heat exchanger. The mass flow rates and the inlet temperatures are given. The rate of heat transfer and the outlet temperatures are to be determined.

Assumptions 1 Steady operating conditions exist. 2 The heat exchanger is well insulated so that heat loss to the surroundings is negligible and thus heat transfer from the hot fluid is equal to the heat transfer to the cold fluid. 3 The thickness of the tube is negligible since it is thin-walled. 4 Changes in the kinetic and potential energies of fluid streams are negligible. 5 The overall heat transfer coefficient is constant and uniform.

Analysis The schematic of the heat exchanger is given in Figure 10-30. The outlet temperatures are not specified, and they cannot be determined from an energy balance. The use of the LMTD method in this case will involve tedious iterations, and thus the  $\varepsilon$ -NTU method is indicated. The first step in the  $\varepsilon$ -NTU method is to determine the heat capacity rates of the hot and cold fluids and identify the smaller one:

$$C_h = \dot{m}_h C_{ph} = (0.3 \text{ kg/s})(2.13 \text{ kJ/kg} \cdot ^{\circ}\text{C}) = 0.639 \text{ kW/}^{\circ}\text{C}$$
  
 $C_c = \dot{m}_c C_{pc} = (0.2 \text{ kg/s})(4.18 \text{ kJ/kg} \cdot ^{\circ}\text{C}) = 0.836 \text{ kW/}^{\circ}\text{C}$ 

Therefore,

$$C_{\min} = C_h = 0.639 \text{ kW/°C}$$

and

20°C

Water

0.2 kg/s

$$C = \frac{C_{\min}}{C_{\max}} = \frac{0.639}{0.836} = 0.764$$

Then the maximum heat transfer rate is determined from Equation 10-32 to be

$$\dot{Q}_{\text{max}} = C_{\text{min}}(T_{h,\text{in}} - T_{c,\text{in}})$$
  
= (0.639 kW/°C)(150 - 20)°C = 83.1 kW

That is, the maximum possible heat transfer rate in this heat exchange 83.1 kW. The heat transfer surface area is

$$A = n(\pi DL) = 8\pi(0.014 \text{ m})(5 \text{ m}) = 1.76 \text{ m}^2$$

Then the NTU of this heat exchanger becomes

150°C Oil 0.3 kg/s

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**FIGURE 10-30** Schematic for Example 10-9.

The effectivenes

We could also d more accurately becomes

Finally, the outle mined to be

$$\dot{Q} = C_c(T_c)$$

$$\dot{Q} = C_h(T_h)$$

Therefore, the te

## 10-6 **■ THE**

Heat exchanger simplified appr ple, we assum throughout the cients can be pi be kept in min exceed 30 perce ers in order to: Heat transf increased press from the enhan the accompany which fluid sho side. Usually, ti Passage area a pressure for the Engineers exchangers to a

The Selection of Heat Exchanges

eat Exchanger

e-passes heat exer with an internal exchanger is 5 mm flows through the ate of 0.3 kg/s. The espectively, Deterputlet temperatures

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t exchanger is well d thus heat transfer 3 The thickness of inetic and potential unsfer coefficients

Figure 10:30 The letermined from an will involve tedious of first step in the hot and cold fluids

kW/°C kW/°C

ation 10-32 to be

W

heat exchanger is

the effectiveness of this heat exchanger corresponding to C=0.764 and C=0.853 is determined from Figure 10-26c to be

$$\varepsilon = 0.47$$

We could also determine the effectiveness from the third relation in Table 10-4 more, accurately but with more labor. Then the actual rate of heat transfer becomes

$$\dot{Q} = \varepsilon \dot{Q}_{\text{max}} = (0.47)(83.1 \text{ kW}) = 39.1 \text{ kW}$$

finally, the outlet temperatures of the cold and the hot fluid streams are determined to be

$$\dot{Q} = C_c (T_{c, \text{out}} - T_{c, \text{in}}) \longrightarrow T_{c, \text{out}} = T_{c, \text{in}} + \frac{\dot{Q}}{C_c}$$

$$= 20^{\circ}\text{C} + \frac{39.1 \text{ kW}}{0.836 \text{ kW/°C}} = 66.8^{\circ}\text{C}$$

$$\dot{Q} = C_h(T_{h, \text{in}} - T_{h, \text{out}}) \longrightarrow T_{h, \text{out}} = T_{h, \text{in}} - \frac{\dot{Q}}{C_h}$$

$$= 150^{\circ}\text{C} - \frac{39.1 \text{ kW}}{0.639 \text{ kW/°C}} = 88.8^{\circ}\text{C}$$

Therefore, the temperature of the cooling water will rise from 20°C to 66.8°C as it cools the hot oil from 150°C to 88.8°C in this heat exchanger.

#### 10:6 ■ THE SELECTION OF HEAT EXCHANGERS

Heat exchangers are complicated devices, and the results obtained with the simplified approaches presented above should be used with care. For example, we assumed that the overall heat transfer coefficient U is constant throughout the heat exchanger and that the convection heat transfer coefficients can be predicted using the convection correlations. However, it should be kept in mind that the uncertainty in the predicted value of U can even exceed 30 percent. Thus, it is natural to tend to overdesign the heat exchangers in order to avoid unpleasant surprises.

Heat transfer enhancement in heat exchangers is usually accompanied by hereased pressure drop, and thus higher pumping power. Therefore, any gain from the enhancement in heat transfer should be weighed against the cost of the accompanying pressure drop. Also, some thought should be given to which fluid should pass through the tube side and which through the shell side Usually, the more viscous fluid is more suitable for the shell side (larger passage area and thus lower pressure drop) and the fluid with the higher passage for the tube side.

Engineers in industry often find themselves in a position to select heat exchangers to accomplish certain heat transfer tasks. Usually, the goal is to

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heat or cool a certain fluid at a known mass flow rate and temperature to desired temperature. Thus, the rate of heat transfer in the prospective heat exchanger is

$$\dot{Q}_{\rm max} = \dot{m}C_p(T_{\rm in} - T_{\rm out})$$

which gives the heat transfer requirement of the heat exchanger before having any idea about the heat exchanger itself.

An engineer going through catalogs of heat exchanger manufactures will be overwhelmed by the type and number of readily available offifice shelf heat exchangers. The proper selection depends on several factors

#### Heat Transfer Rate

This is the most important quantity in the selection of a heat exchanger A heat exchanger should be capable of transferring heat at the specified rate in order to achieve the desired temperature change of the fluid at the specified mass flow rate.

#### Cost

Budgetary limitations usually play the most important role in the selection heat exchangers, except for some specialized cases where "money is not ject." An off-the-shelf heat exchanger has a definite cost advantage over those made to order. However, in some cases, none of the existing health changers will do, and it may be necessary to undertake the expensive and time-consuming task of designing and manufacturing a heat exchanger from scratch to suit the needs. This is often the case when the heat exchanger is an integral part of the overall device to be manufactured.

The operation and maintenance costs of the heat exchanger are also important considerations in assessing the overall cost.

#### **Pumping Power**

In a heat exchanger, both fluids are usually forced to flow by pumps of the that consume electrical power. The annual cost of electricity associated with the operation of the pumps and fans can be determined from

Operating cost = (Pumping power, kW) × (Hours of operation, h)

× (Price of electricity, \$/kWh)

where the pumping power is the total electrical power consumed by motors of the pumps and fans. For example, a heat exchanger that involves 1-hp pump and a  $\frac{1}{3}$ -hp fan (1 hp = 0.746 kW) operating 8 h a day and 5 days a week will consume 2017 kWh of electricity per year, which will cost \$160 at an electricity cost of 8 cents/kWh.

Minimizing the pressure drop and the mass flow rate of the fluids will minimize the operating cost of the heat exchanger, but it will maximize the size of the heat exchanger and thus the initial cost. As a rule of thumb doubling the mass flow rate will reduce the initial cost by half but will be crease the pumping power requirements by a factor of roughly eight;

Typically, flui 07 and 7 m/s for are helpful in avo ্রাক্ত্র

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Sizeand Weight Normally, the smu is especially the c and weight requi normally carries changer in some

The type of heat fluids involved, th change processes by a gas if the su side. On the oth suitable for cooli

#### Materials

The materials u important consid thermal and stru low 15 atm or ter erations above 7 of the heat excha

A temperat the shell will pr needs to be cons expensive corro. nium if we are n

Other Consider There are other Or may not be in leak-tight is an involved. Ease ( @some other is one of the p exchangers usec

EXAMPLE 10-1( വരില്റ്റ് plant, nace. The hot wa **Elemin.** The r en efficiency of (105, temperature to prospective the

Typically, fluid velocities encountered in heat exchangers range between 3 and 7 m/s for liquids and between 3 and 30 m/s for gases. Low velocities nelpful in avoiding erosion, tube vibrations, and noise as well as pressure

The Selection of Heat Exchangers

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it will maximize the As a rule of thurs to by half but will be roughly eight.

## Size and Weight

Normally, the smaller and the lighter the heat exchanger, the better it is. This is especially the case in the automotive and aerospace industries, where size and weight requirements are most stringent. Also, a larger heat exchanger normally carries a higher price tag. The space available for the heat exchanger in some cases limits the length of the tubes that can be used.

The type of heat exchanger to be selected depends primarily on the type of fuids involved, the size and weight limitations, and the presence of any phase-change processes. For example, a heat exchanger is suitable to cool a liquid by a gas if the surface area on the gas side is many times that on the liquid side. On the other hand, a plate or shell-and-tube heat exchanger is very suitable for cooling a liquid by another liquid.

#### Materials

The materials used in the construction of the heat exchanger may be an important consideration in the selection of heat exchangers. For example, the thermal and structural stress effects need not be considered at pressures below 15 atm or temperatures below 150°C. But these effects are major considerations above 70 atm or 550°C and seriously limit the acceptable materials of the heat exchanger.

A temperature difference of 50°C or more between the tubes and the shell will probably pose differential thermal expansion problems and needs to be considered. In the case of corrosive fluids, we may have to select expensive corrosion-resistant materials such as stainless steel or even titanium if we are not willing to replace low-cost heat exchangers frequently.

#### Other Considerations

There are other considerations in the selection of heat exchangers that may coming not be important, depending on the application. For example, being lakitight is an important consideration when toxic or expensive fluids are an important consideration when toxic or expensive fluids are some other important considerations in the selection process. Quietness some of the primary considerations in the selection of liquid-to-air heat exchangers used in heating and air-conditioning applications.

EXAMPLE 10-10 Installing a Heat Exchanger to Save Energy and Money

ma dairy plant, milk is pasteurized by hot water supplied by a natural gas furace. The hot water is then discharged to an open floor drain at 80°C at a rate of 5 kg/min. The plant operates 24 h a day and 365 days a year. The furnace has a efficiency of 80 percent, and the cost of the natural gas is \$0.40 per therm of the cold water entering the Marie Property Company

**CHAPTER 10 Heat Exchangers** 

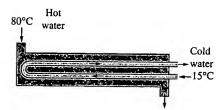


FIGURE 10-31 Schematic for Example 10-10.

furnace throughout the year is 15°C. The drained hot water cannot be returned. the furnace and recirculated, because it is contaminated during the process

In order to save energy, installation of a water-to-water heat exchange preheat the incoming cold water by the drained hot water is proposed. Assum that the heat exchanger will recover 75 percent of the available heat in the water, determine the heat transfer rating of the heat exchanger that needs to be purchased and suggest a suitable type. Also, determine the amount of mo this heat exchanger will save the company per year from natural gas savings

**Solution** A water-to-water heat exchanger is to be installed to transfer energy from drained hot water to the incoming cold water to preheat it. The rate of heat transfer in the heat exchanger and the amount of energy and money saved year are to be determined.

Assumptions 1 Steady operating conditions exist. 2 The effectiveness of the heat exchanger remains constant. -

**Properties** We use the specific heat of water at room temperature,  $C_p = 4.18$ kg · °C (Table A-9), and treat it as a constant.

Analysis A schematic of the prospective heat exchanger is given in Figure 10-31. The heat recovery from the hot water will be a maximum when it less the heat exchanger at the inlet temperature of the cold water. Therefore,

$$\dot{Q}_{\text{max}} = \dot{m}_h C_p (T_{h, \text{in}} - T_{c, \text{in}})$$

$$= \left(\frac{15}{60} \text{ kg/s}\right) (4.18 \text{ kJ/kg} \cdot ^{\circ}\text{C}) (80 - 15)^{\circ}\text{C}$$

$$= 67.9 \text{ kJ/s}$$

That is, the existing hot water stream has the potential to supply heat at a'r 67.9 kJ/s to the incoming cold water. This value would be approached in a counter-flow heat exchanger with a very large heat transfer surface area. A heat exchanger of reasonable size and cost can capture 75 percent of this heat transfer potential. Thus, the heat transfer rating of the prospective heat exchange must be

$$\dot{Q} = \varepsilon \dot{Q}_{\text{max}} = (0.75)(67.9 \text{ kJ/s}) =$$
**50.9 kJ/s**

That is, the heat exchanger should be able to deliver heat at a rate of 50.9144 from the hot to the cold water. An ordinary plate or shell-and-tube heat exchange should be adequate for this purpose, since both sides of the heat exchange involve the same fluid at comparable flow rates and thus comparable heat trans fer coefficients. (Note that if we were heating air with hot water, we would have specify a heat exchanger that has a large surface area on the air side.)

The heat exchanger will operate 24 h a day and 365 days a year. There the annual operating hours are

Noting that this heat exchanger saves 50.9 kJ of energy per second, the saved during an entire year will be

Energy saved = (Heat transfer rate)(Operation time)  
= 
$$(50.9 \text{ kJ/s})(8760 \text{ h/year})(3600 \text{ s/h})$$
  
=  $1.605 \times 10^9 \text{ kJ/year}$ 

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Therefore, the insta 37607 a year, and paid from the fuel s

## 10:72 SUMM

Heat exchangers fluids without all manufactured in : exchanger. In a pc exchanger at the counter-flow type ends and flow in fluids move perp called cross-flow. plications are the Heat transfer and conduct sisof heat exchai coefficient U or a

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ce is said to be 80-percent efficient. That is, for each 80 units of heat the furnace, natural gas with an energy content of 100 units must be the furnace. Therefore, the energy savings determined above result vings in the amount of

Energy saved = 
$$\frac{\text{Energy saved}}{\text{Furnace efficiency}} = \frac{1.605 \times 10^9 \text{ kJ/year}}{0.80} \left(\frac{1 \text{ therm}}{105,500 \text{ kJ}}\right)$$
  
= 19,020 therms/year

therm = 105,500 kJ. Noting that the price of natural gas is \$0.40 per he amount of money saved becomes

merefore the installation of the proposed heat exchanger will save the company 1007 a year, and the installation cost of the heat exchanger will probably be he fuel savings in a short time.

## 070 SUMMARY

matexchangers are devices that allow the exchange of heat between two mits without allowing them to mix with each other. Heat exchangers are manufactured in a variety of types, the simplest being the double-pipe heat ochanger. In a parallel-flow type, both the hot and cold fluids enter the heat r at the same end and move in the same direction, whereas in a achanger at the same end and move in the same direction, whereas in a counter-flow type, the hot and cold fluids enter the heat exchanger at opposite and flow in opposite directions. In compact heat exchangers, the two hids move perpendicular to each other, and such a flow configuration is alled eross-flow. Other common types of heat exchangers in industrial apdications are the plate and the shell-and-tube heat exchangers.

Heat transfer in a heat exchanger usually involves convection in each midand conduction through the wall separating the two fluids. In the analysofheat exchangers, it is convenient to work with an overall heat transfer wifficient U or a total thermal resistance R, expressed as

$$\frac{1}{UA} = \frac{1}{U_i A_i} = \frac{1}{U_o A_o} = R = \frac{1}{h_i A_i} + R_{\text{wall}} + \frac{1}{h_o A_o}$$

thereithe subscripts i and o stand for the inner and outer surfaces of the wall separates the two fluids, respectively. When the wall thickness of the delistimall and the thermal conductivity of the tube material is high, the boverelation simplifies to

$$\frac{1}{U} \approx \frac{1}{h_i} + \frac{1}{h_o}$$

 $U_i \approx U_i \approx U_o$ . The effects of fouling on both the inner and the outer faces of the tubes of a heat exchanger can be accounted for by

Summary

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CHAPTER 10 Heat Exchangers

$$\frac{1}{UA} = \frac{1}{U_i A_i} = \frac{1}{U_o A_o} = R = \frac{1}{h_i A_i} + \frac{R_{f,i}}{A_i} + \frac{\ln(D_o/D_i)}{2\pi kL} + \frac{R_{f,o}}{A_o} + \frac{1}{h_o A_o}$$

where  $A_i = \pi D_i L$  and  $A_o = \pi D_o L$  are the areas of the inner and outer surfaces and  $R_{f,i}$  and  $R_{f,o}$  are the fouling factors at those surfaces.

In a well-insulated heat exchanger, the rate of heat transfer from the fluid is equal to the rate of heat transfer to the cold one. That is,

$$\dot{Q} = \dot{m}_c C_{pc} (T_{c,\text{out}} - T_{c,\text{in}}) = C_c (T_{c,\text{out}} - T_{c,\text{in}})$$

and

$$\dot{Q} = \dot{m}_h C_{ph} (T_{h,\text{in}} - T_{h,\text{out}}) = C_h (T_{h,\text{in}} - T_{h,\text{out}})$$

where the subscripts c and h stand for the cold and hot fluids, respectively and the product of the mass flow rate and the specific heat of a fluid c is called the *heat capacity rate*.

Of the two methods used in the analysis of heat exchangers, the log mem temperature difference (or LMTD) method is best suited for determining the size of a heat exchanger when all the inlet and the outlet temperatures are known. The effectiveness-NTU method is best suited to predict the outlet temperatures of the hot and cold fluid streams in a specified heat exchanger. In the LMTD method, the rate of heat transfer is determined from

$$\dot{Q} = UA\Delta T_{\rm lm}$$

where

$$\Delta T_{\rm lm} = \frac{\Delta T_1 - \Delta T_2}{\ln(\Delta T_1 / \Delta T_2)}$$

is the log mean temperature difference, which is the suitable form of the average temperature difference for use in the analysis of heat exchangers. Here  $\Delta T_1$  and  $\Delta T_2$  represent the temperature differences between the two fluids at the two ends (inlet and outlet) of the heat exchanger. For cross-flow and multipass shell-and-tube heat exchangers, the logarithmic mean temperature difference is related to the counter-flow one  $\Delta T_{\text{lm.CF}}$  as

$$\Delta T_{\rm lm} = F \Delta T_{\rm lm,\it CF}$$

where F is the *correction factor*, which depends on the geometry of the head exchanger and the inlet and outlet temperatures of the hot and streams.

The effectiveness of a heat exchanger is defined as

$$\varepsilon = \frac{\dot{Q}}{\dot{Q}_{\text{max}}} = \frac{\text{Actual heat transfer rate}}{\text{Maximum possible heat transfer rate}}$$

where

$$\dot{Q}_{\rm max} = C_{\rm min}(T_{h,\rm in} - T_{c,\rm in})$$

and  $C_{\min}$  is the smaller of  $C_h = \dot{m}_h C_{ph}$  and  $C_c = \dot{m}_c C_{pc}$ . The effectiveness of heat exchangers can be determined from effectiveness relations or change.

The selection such as the heat tr type, materials, ar

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suitable form of the s of heat exchanger ces between the (wo anger. For cross-flow rithmic mean temper CF as

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The effectiveness of elations or charts.

The selection or design of a heat exchanger depends on several factors the heat transfer rate, cost, pressure drop, size, weight, construction materials, and operating environment.

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